

# Dynamic meteorology without tears

## Part III a:

# Rossby's planetary waves

# Can we *see* Rossby waves?

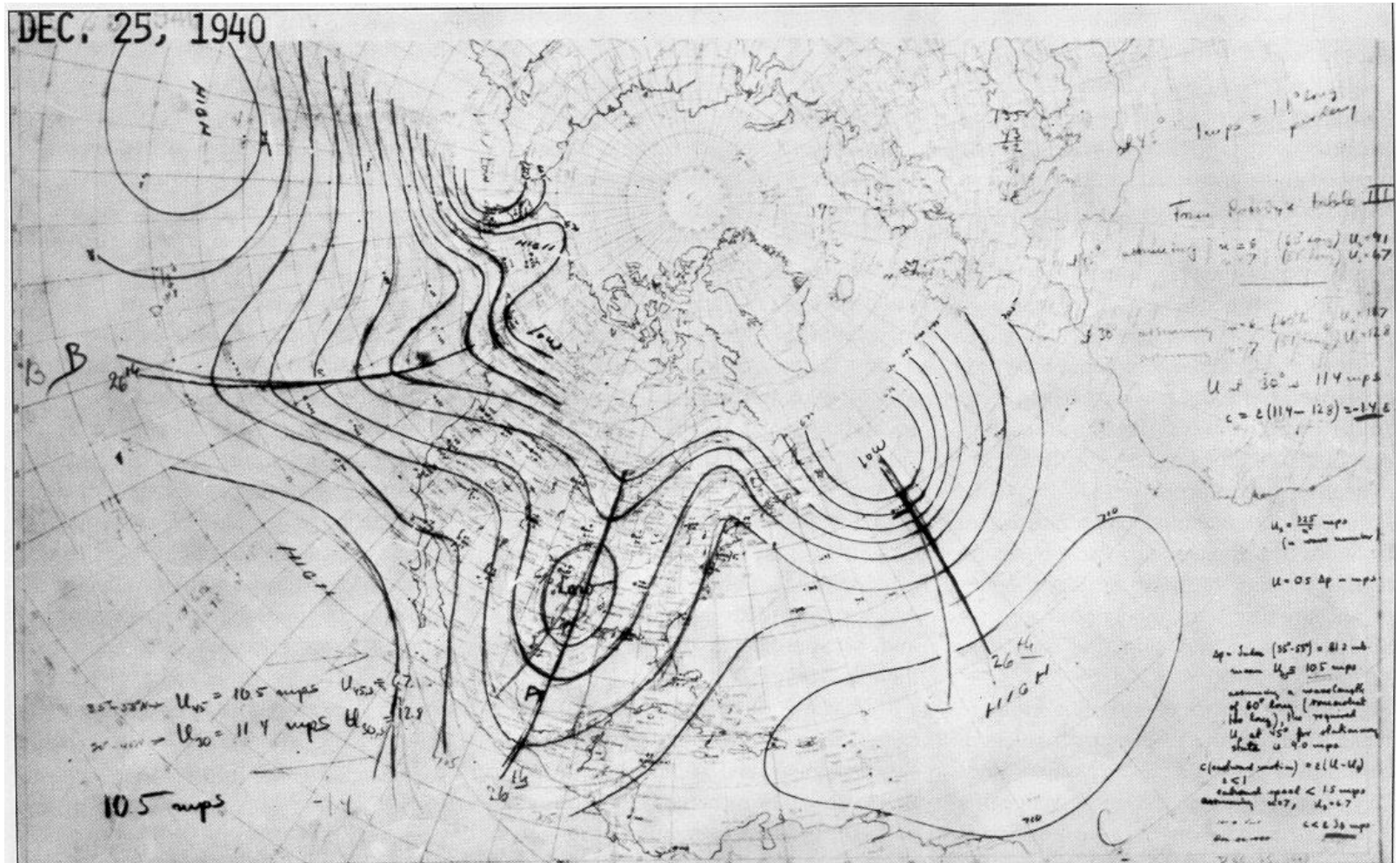
Lunch discussion at ECMWF 1995:

**Scientist: -How is the weekend going to be?**

**AP: -Fine, a Rossby wave is seen coming in!**

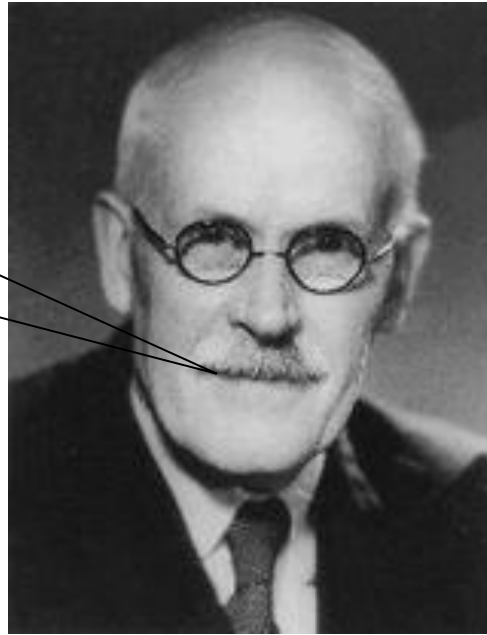
**Scientist: -But can you *see* Rossby waves??**

**-Well, Rossby could see them - at least on Christmas Day 1940**



# What is a Rossby wave?

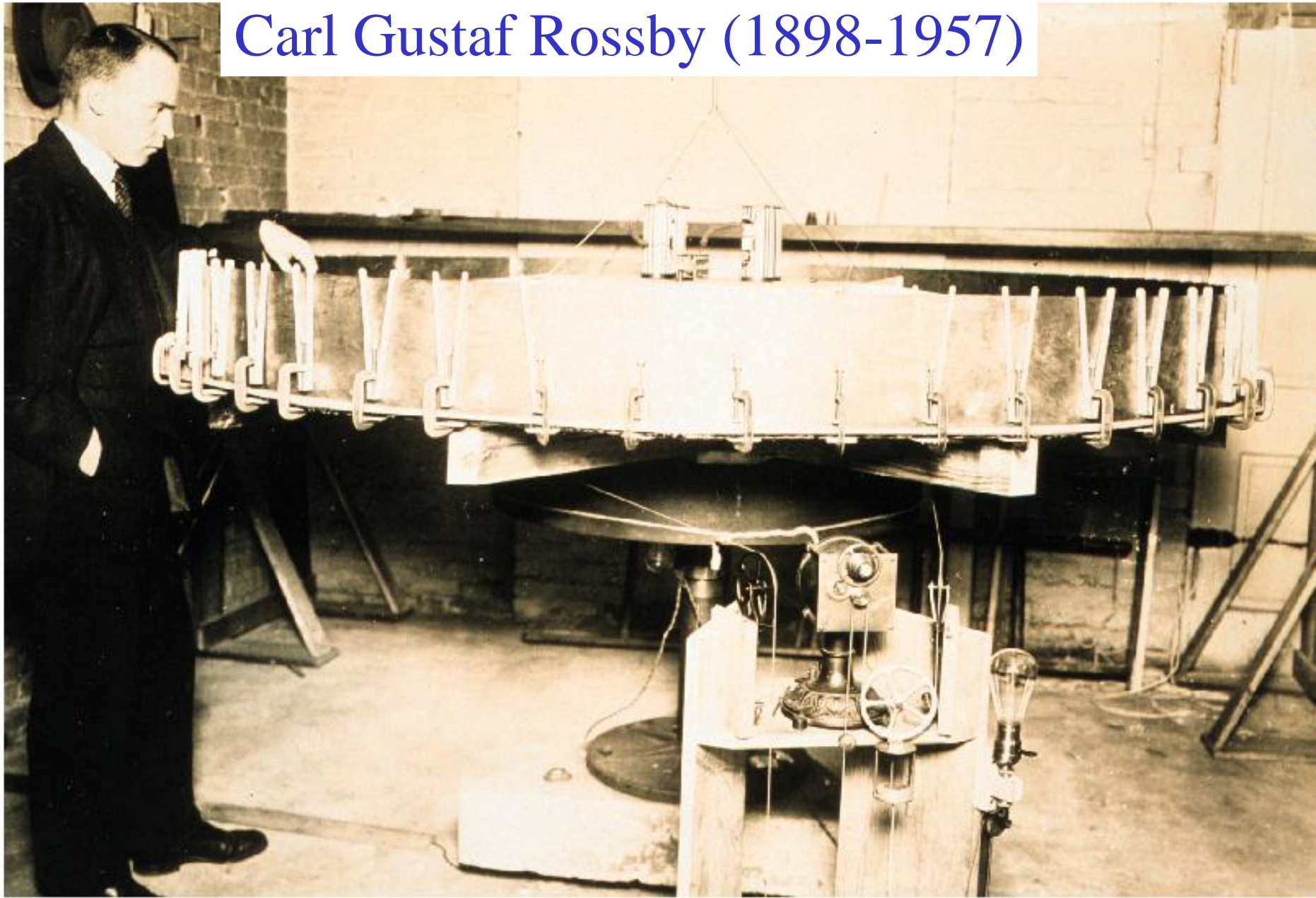
I never  
understood what a  
Rossby wave  
was...



Sir Harold Jeffreys 1891-1989



# Carl Gustaf Rossby (1898-1957)





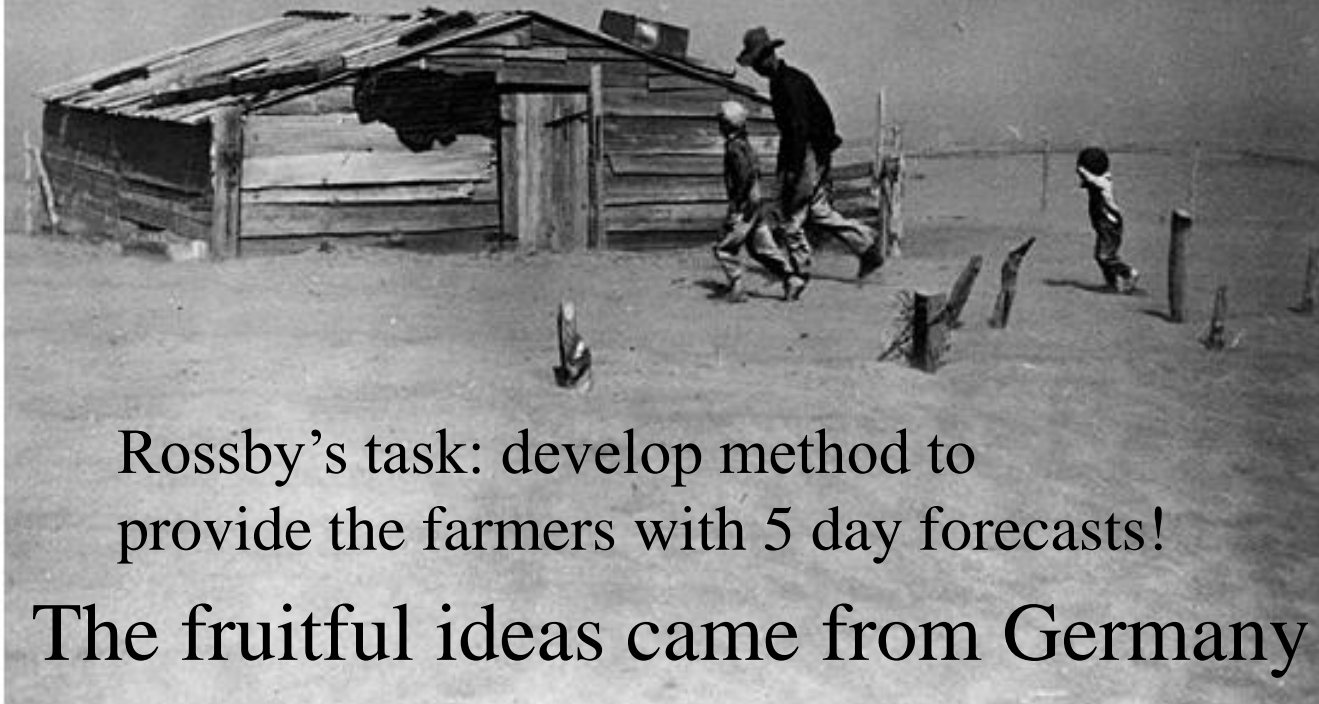
# Carl Gustaf Rossby (1898-1957)



- 1898 Born in Stockholm, Sweden
- 1919-20 Bjerknes group in Bergen
- 1921 Studying aerology in Germany
- 1922-25 Weather forecaster at SMHI
- 1926 Moves to the United States of America to spread the Bergen school concept
- 1936-38 Works on geostrophic adjustment problems
- 1938-39 Discovers and explains “his” wave



# The Dust Bowl draught years in the US mid-west during the 1930's



Rossby's task: develop method to  
provide the farmers with 5 day forecasts!

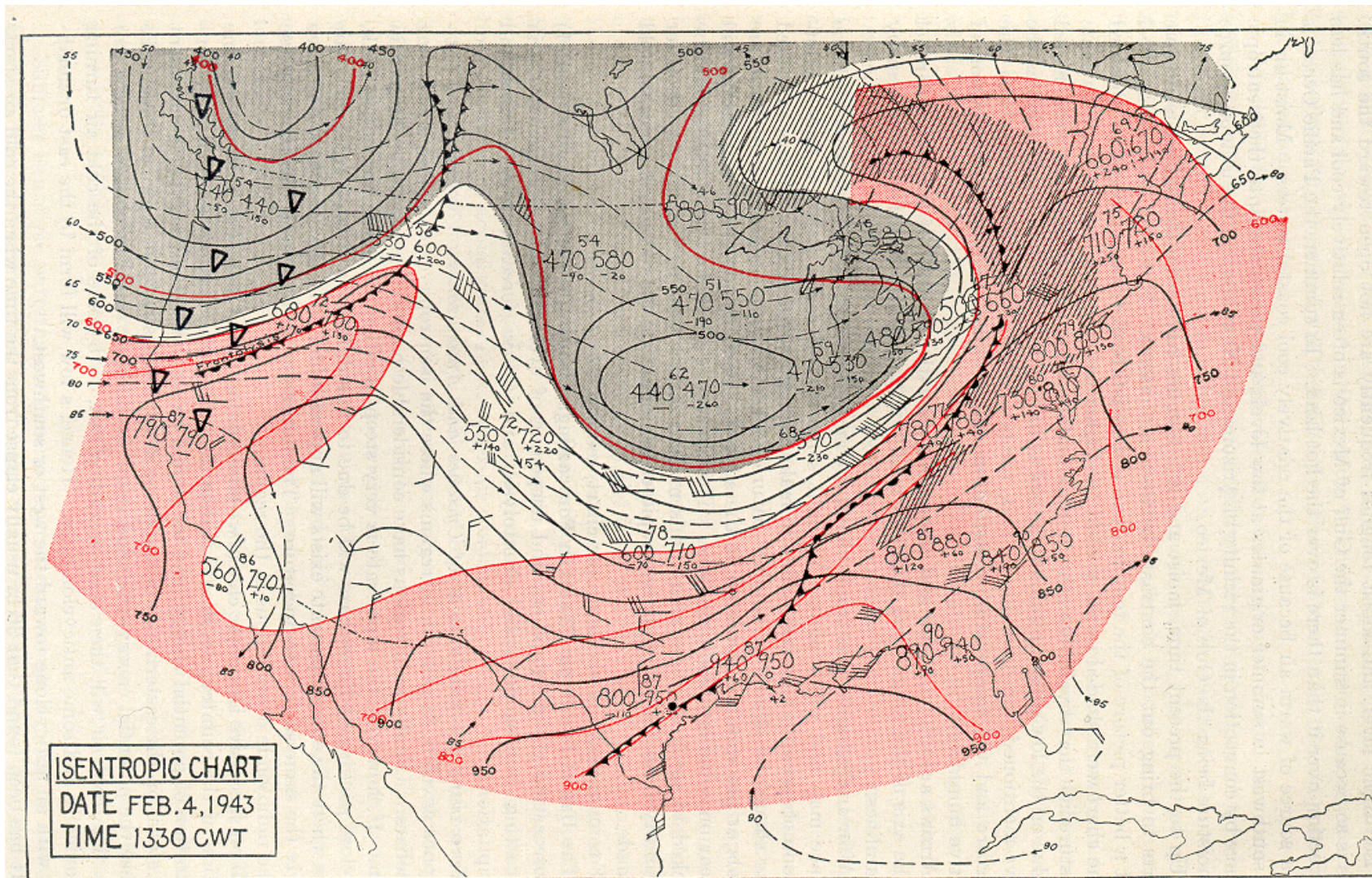
The fruitful ideas came from Germany



# Five-day forecasts from August 1940

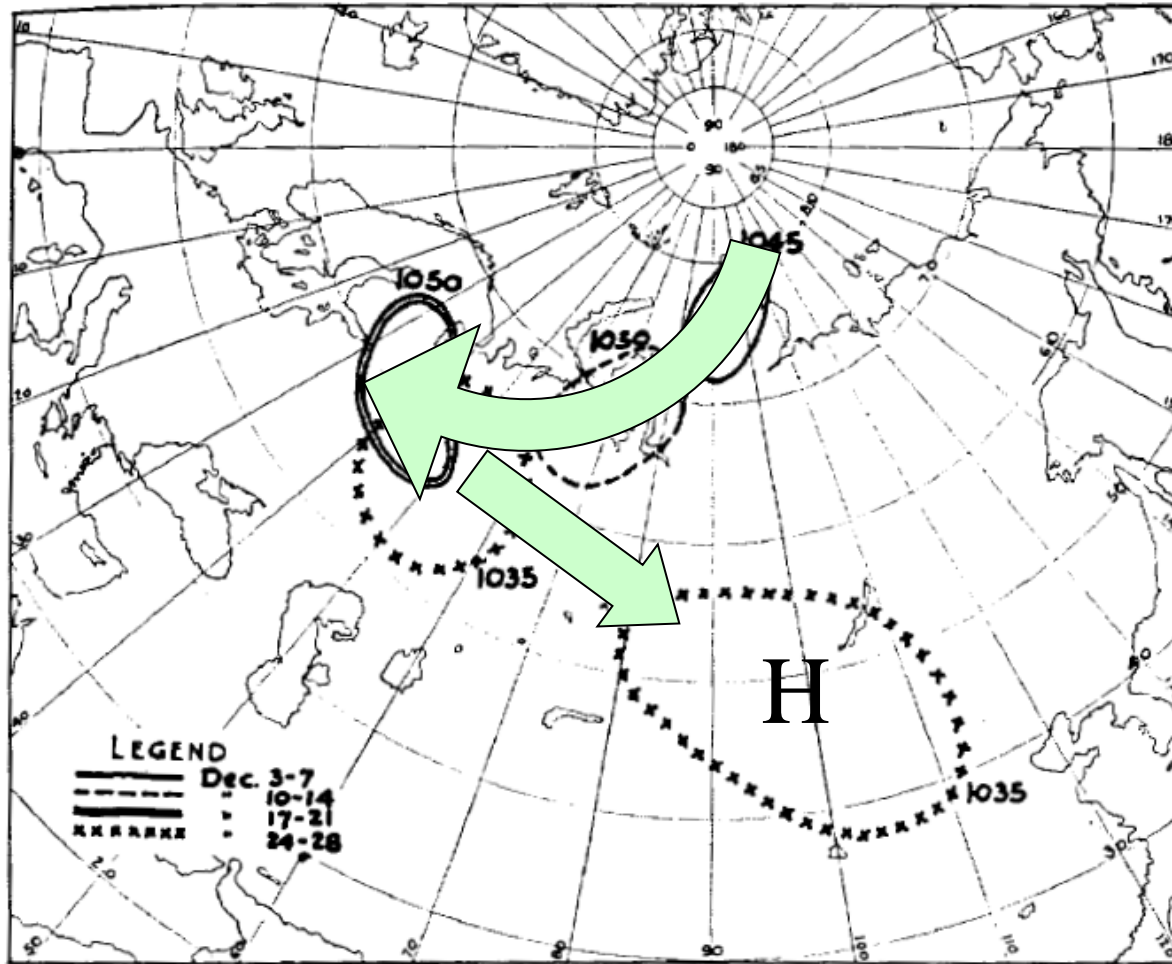




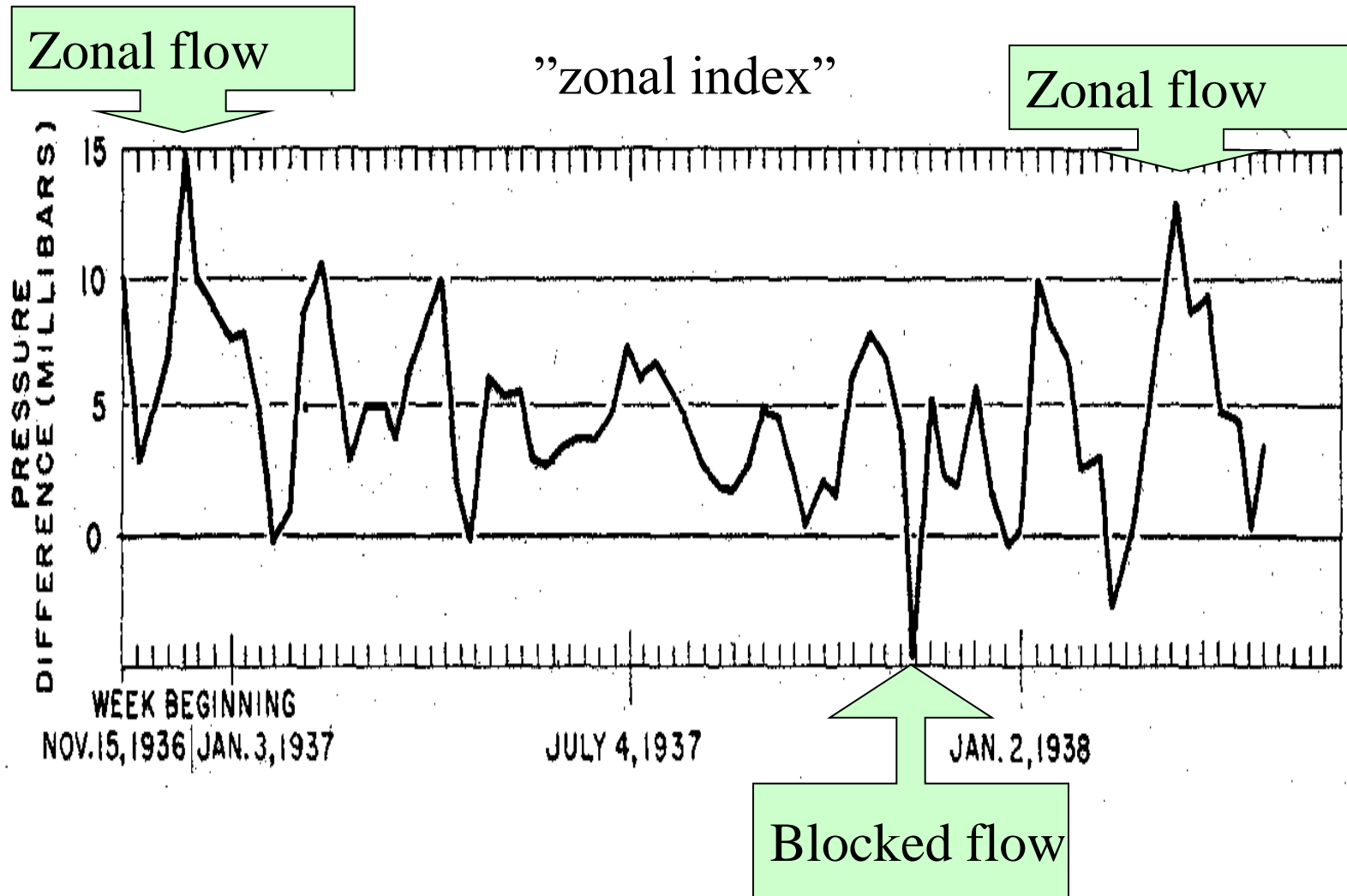




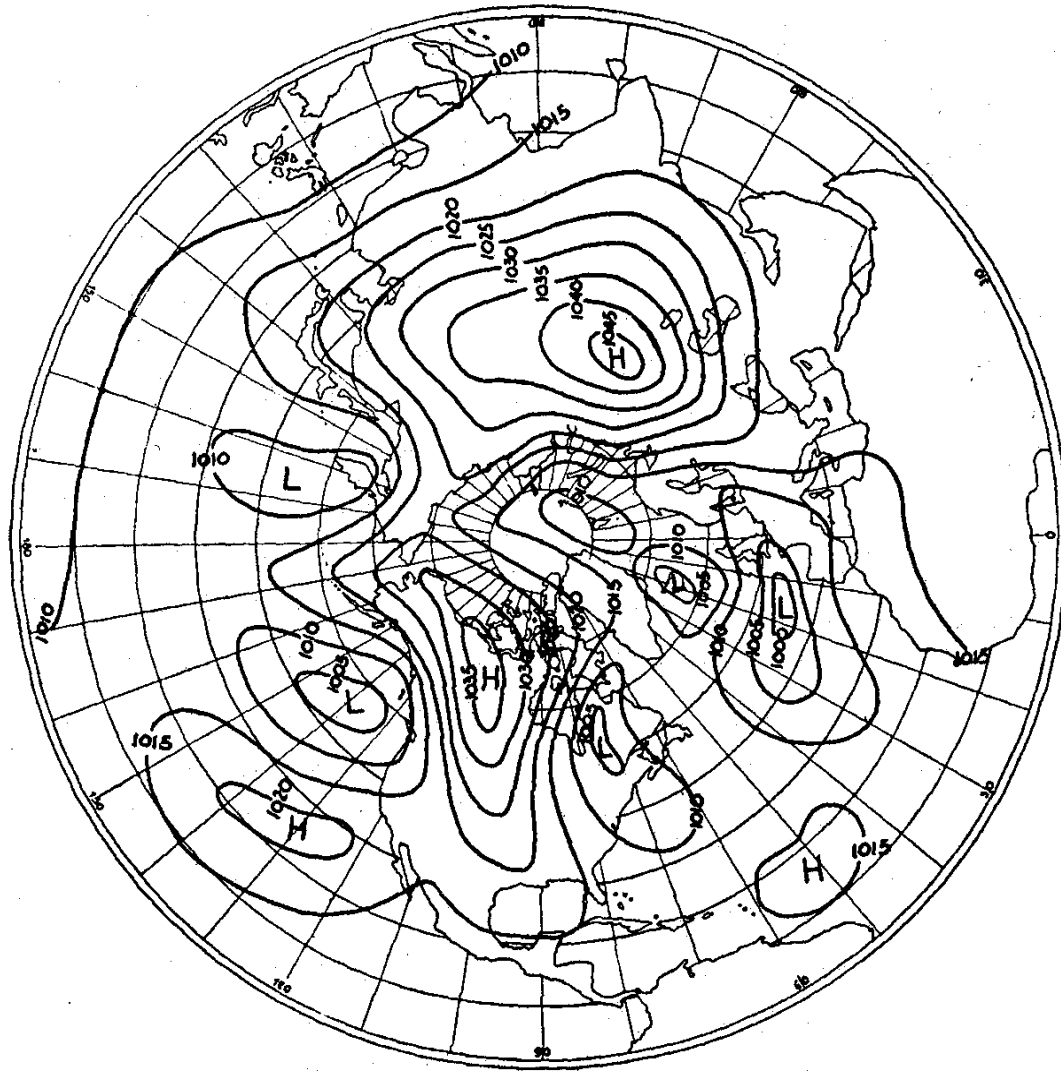
# Motions of the Siberian high Dec 1938



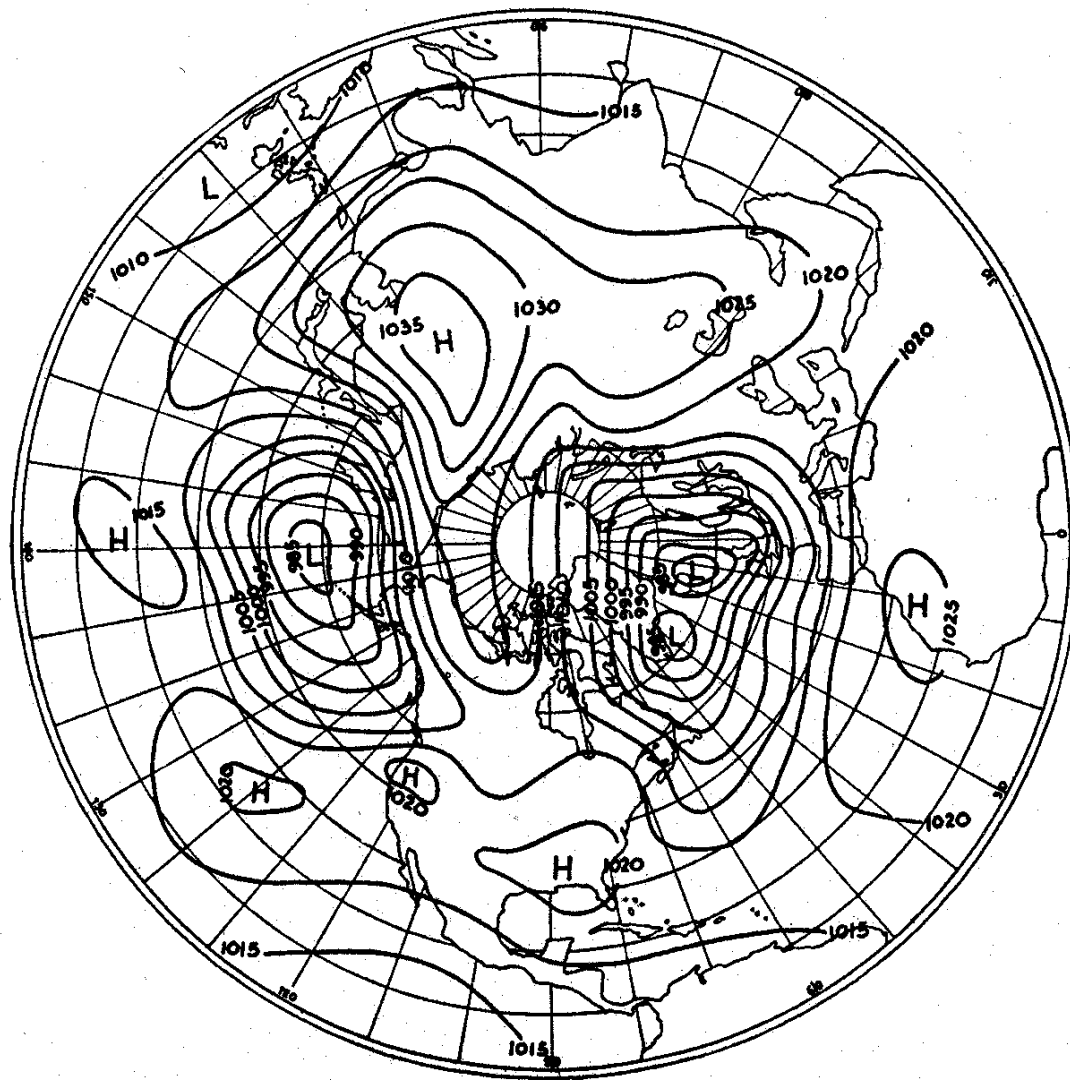
# Pressure difference between 35° and 55° latitude







Low Index  
Circulation  
14-20 Nov  
1937  
**Blocked  
Flow**



High Index  
Circulation  
9-15 Jan  
1938

# Zonal Flow

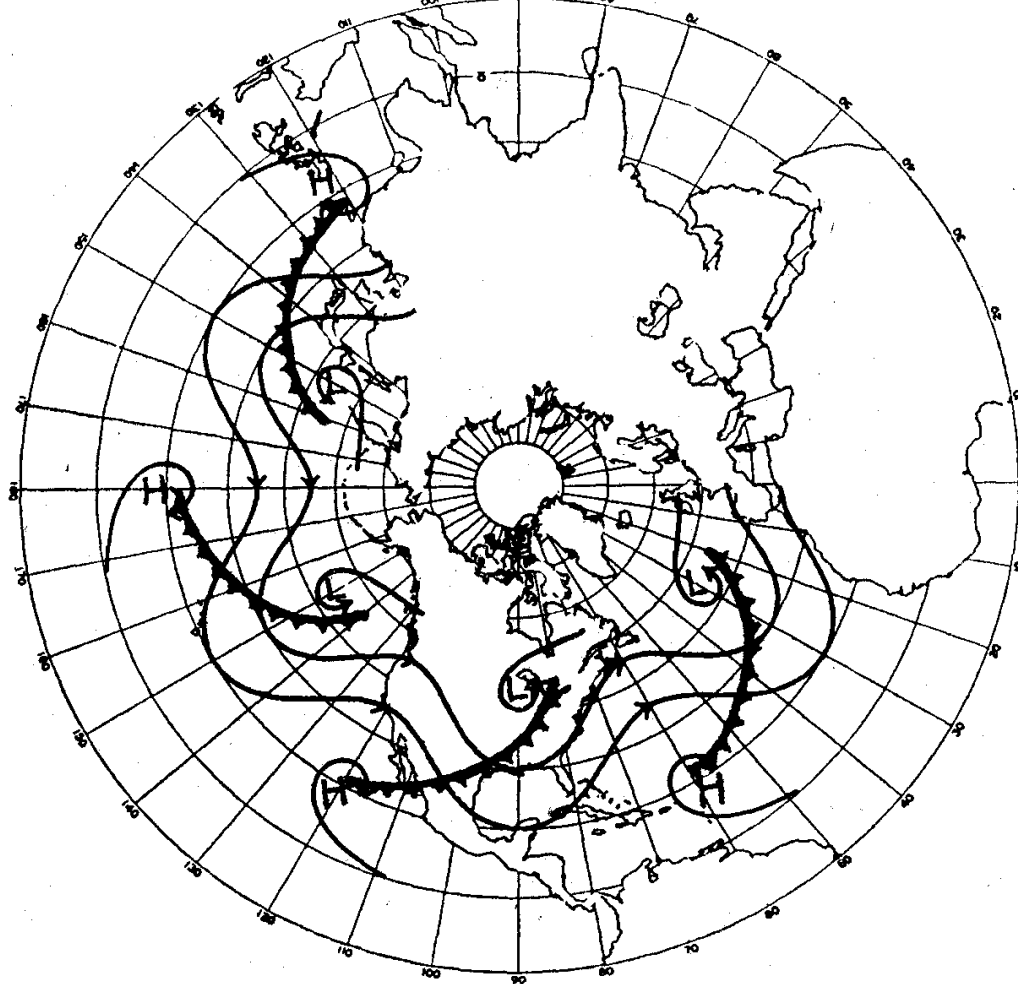
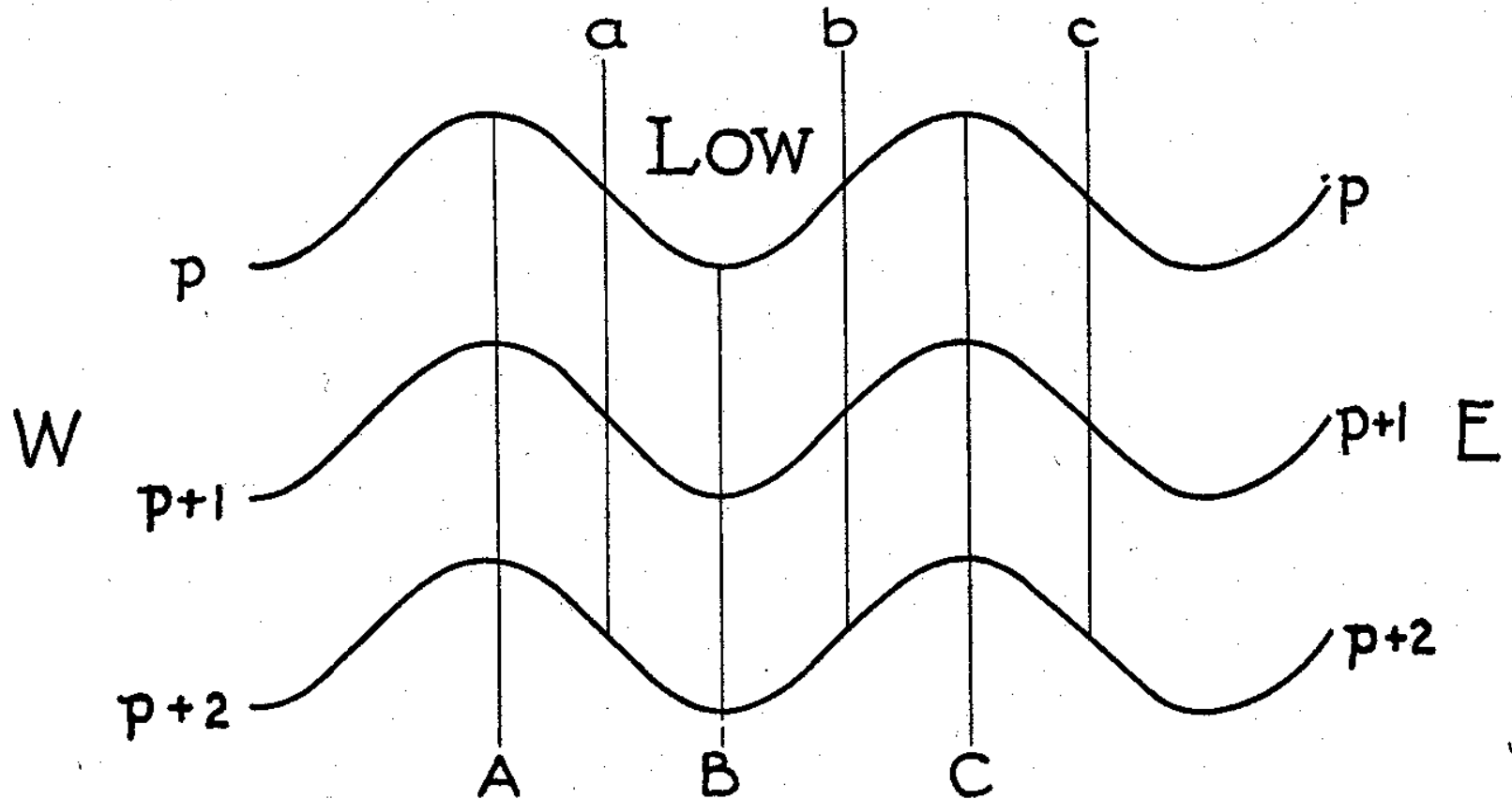


FIGURE 15.—An example of the theoretical planetary flow pattern for weak zonal circulation. Compare this diagram with figure 14 and note the presence in both of a split Aleutian low and a split Icelandic low, with one branch centered over eastern North America. In comparing the two diagrams it should be remembered that the wave pattern of the westerlies indicated here is in reality (fig. 14) obscured by shallow cold-air anticyclones but that it would appear clearly on a corresponding chart for the 3-kilometer level.



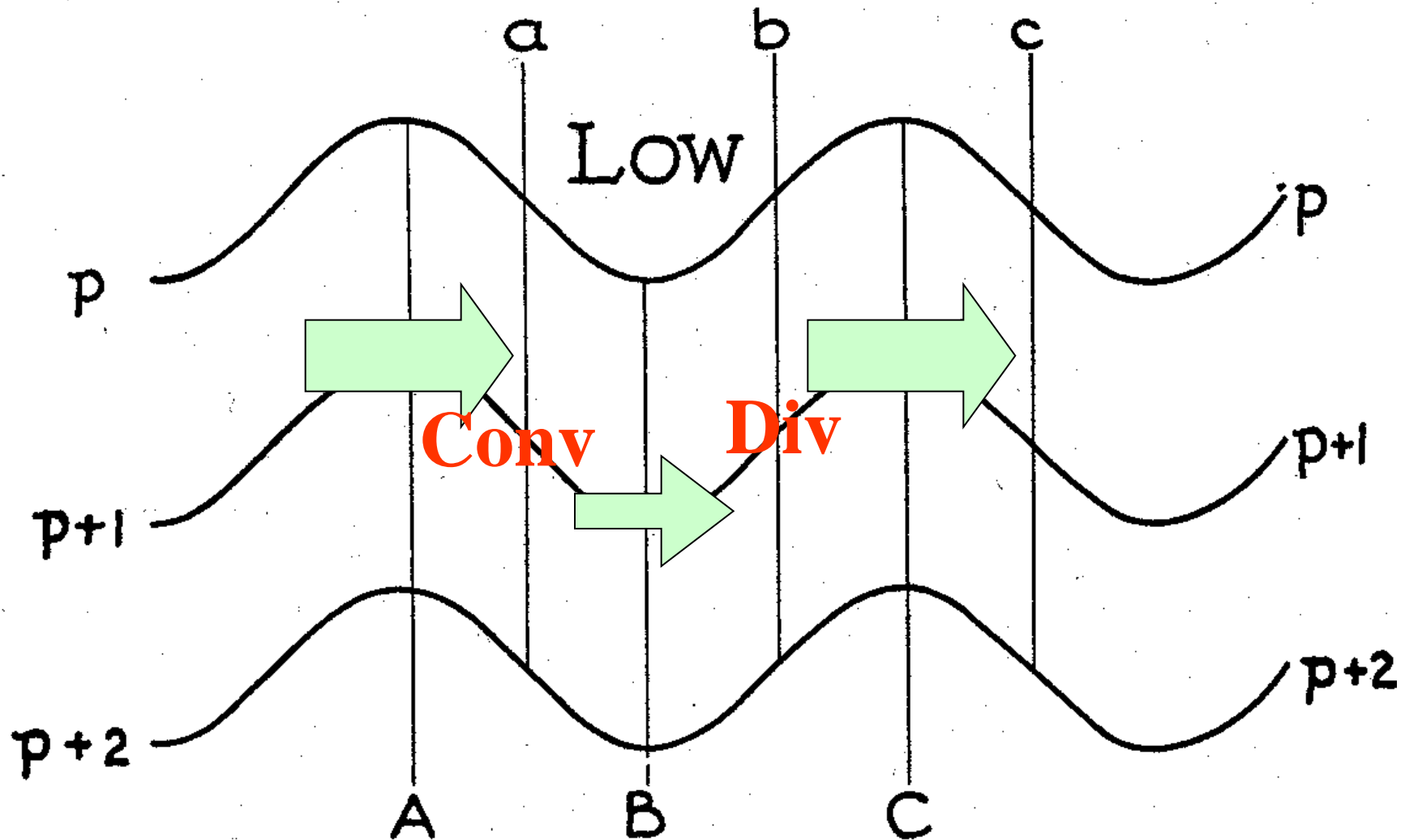
# But what "is" it?

## The isobaric channel illustration used by Rossby et al (1939)



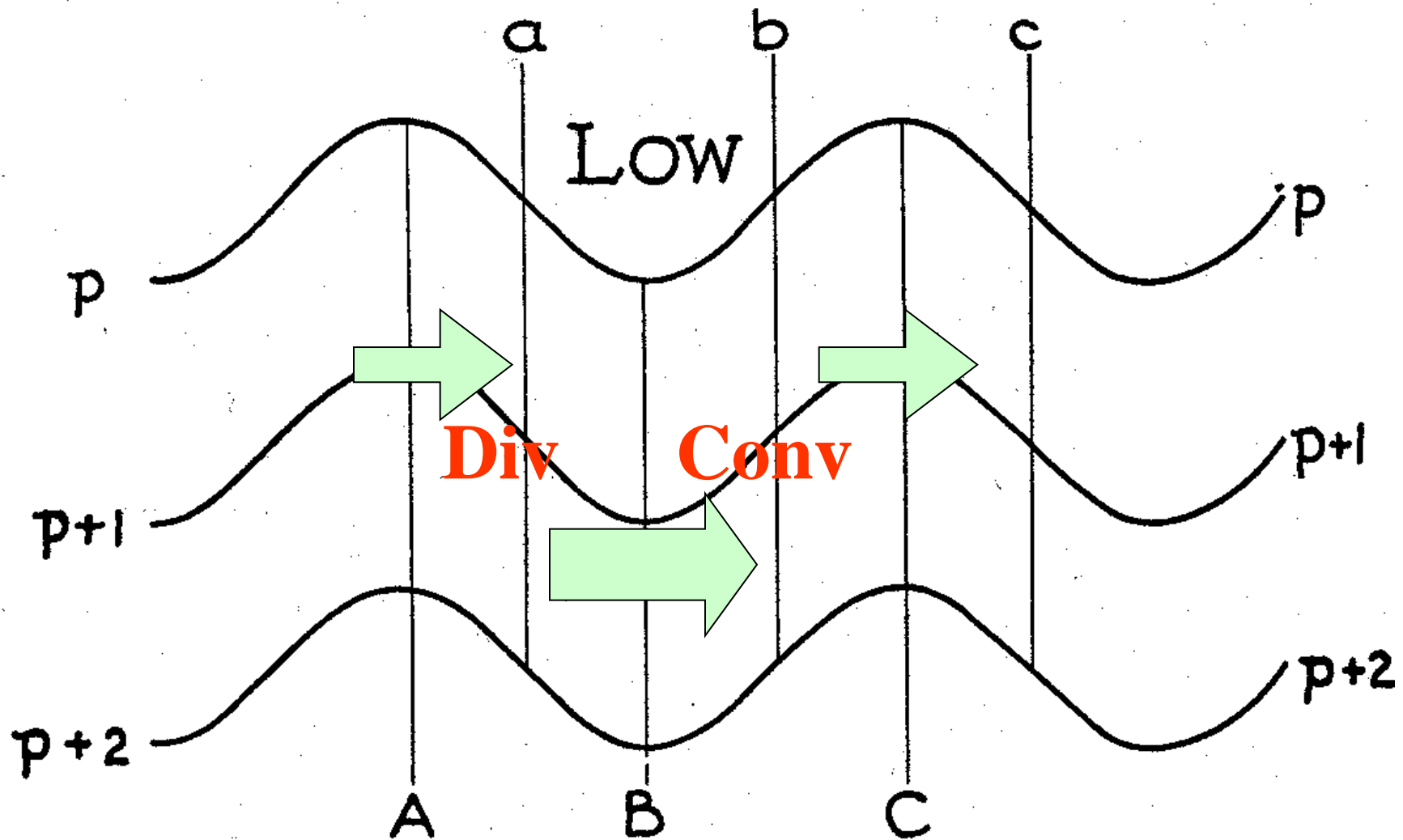
...to which he applied the gradient wind equation

Considering only the curvature effect on the gradient wind which is relevant for shorter waves





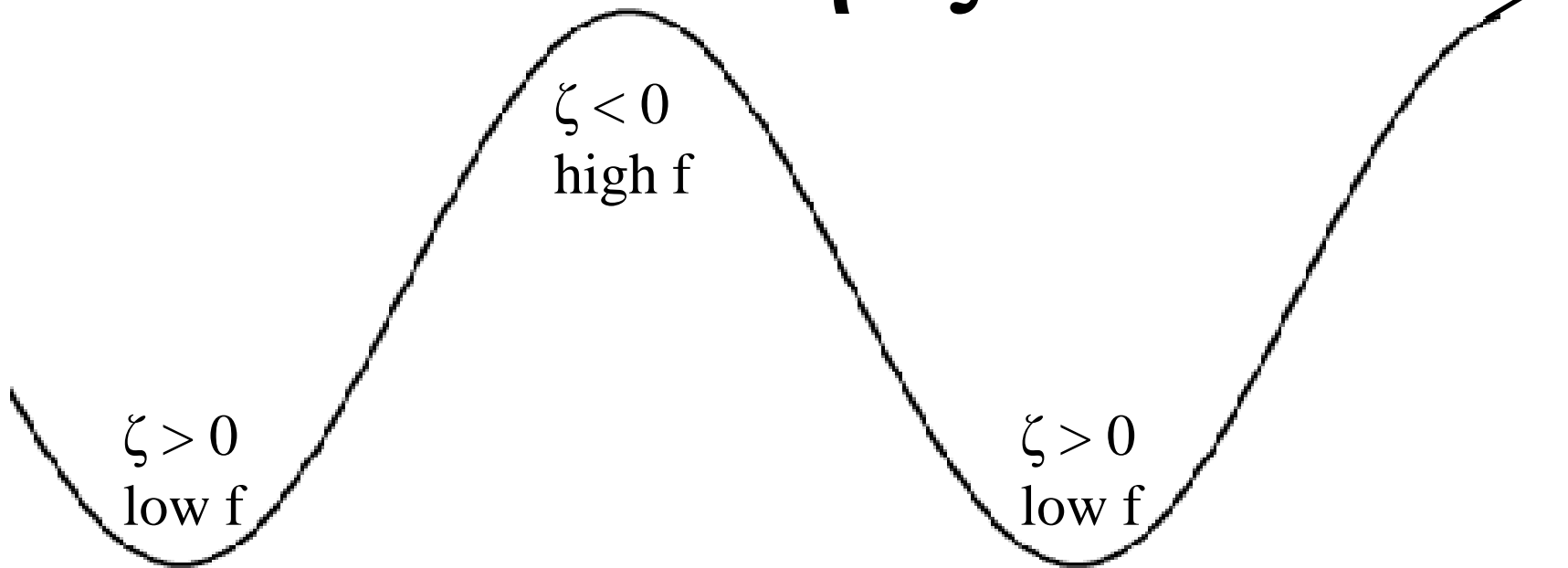
Considering only the latitude effect on the gradient wind  
which is relevant for longer waves



**Only when the paper was published did Rossby realize that he could not use gradient wind balance - it is only applicable on stationary patterns**

In his mathematics Rossby made use of Constant Absolute Vorticity Trajectory (*which is NOT a Rossby wave*)

$$\eta = \zeta + f = \text{const}$$

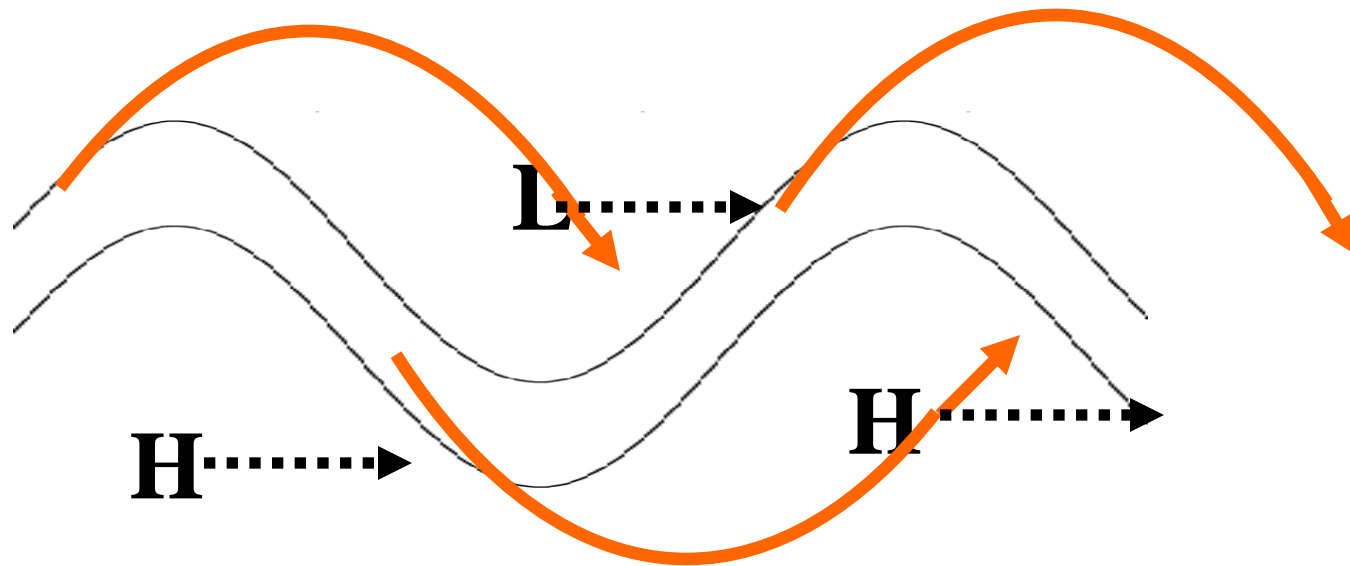


...from which he derived his famous wave formula →

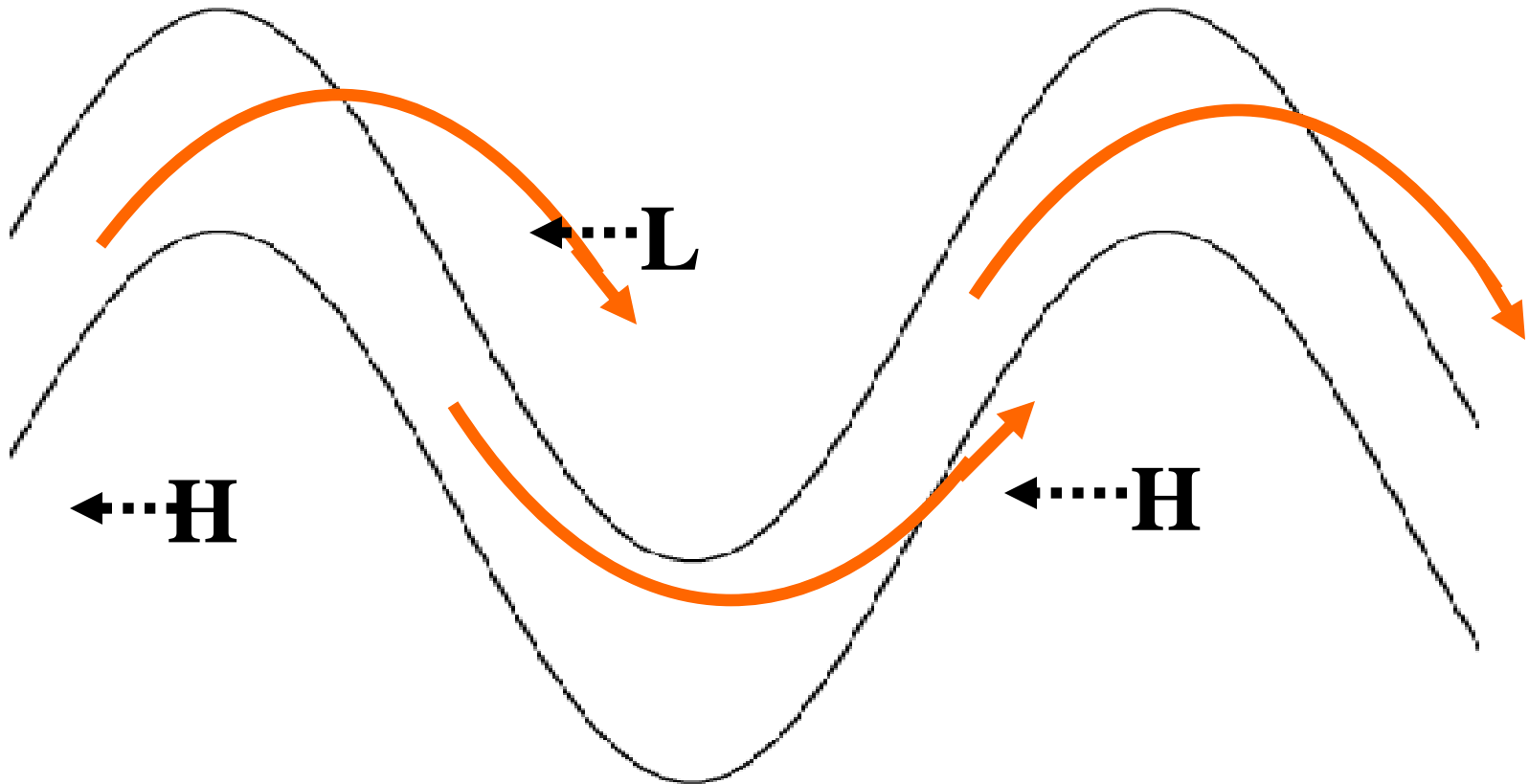


Confusion between  
streamlines (waves) and  
trajectories has always been  
one of the main roots of  
confusion in dynamic and  
synoptic meteorology

# Trajectories associated with low amplitude, short wave length stream lines in a *progressive* flow



# Trajectories associated with high amplitude, long wave length stream lines in a *retrogressive* flow



# Dynamic meteorology without tears

## Part III b:

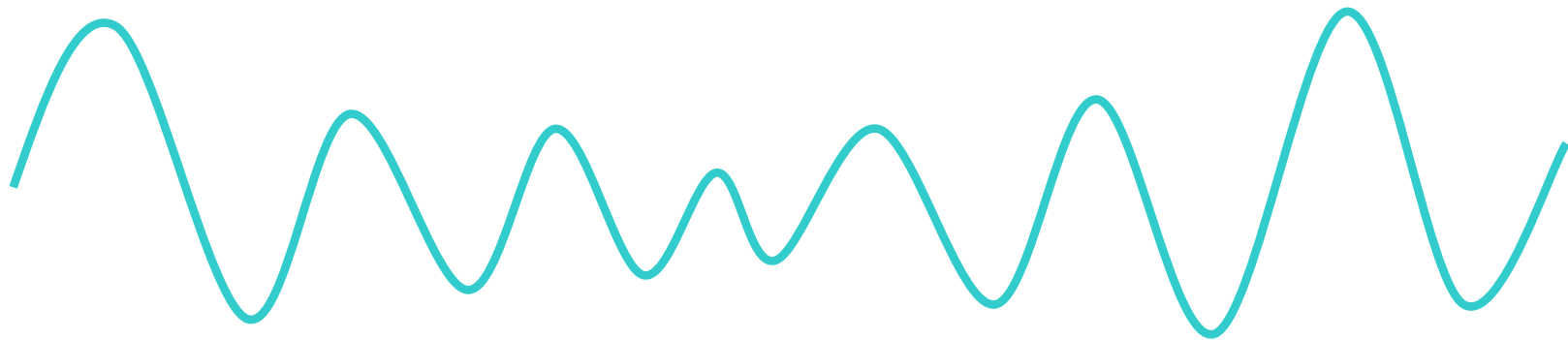
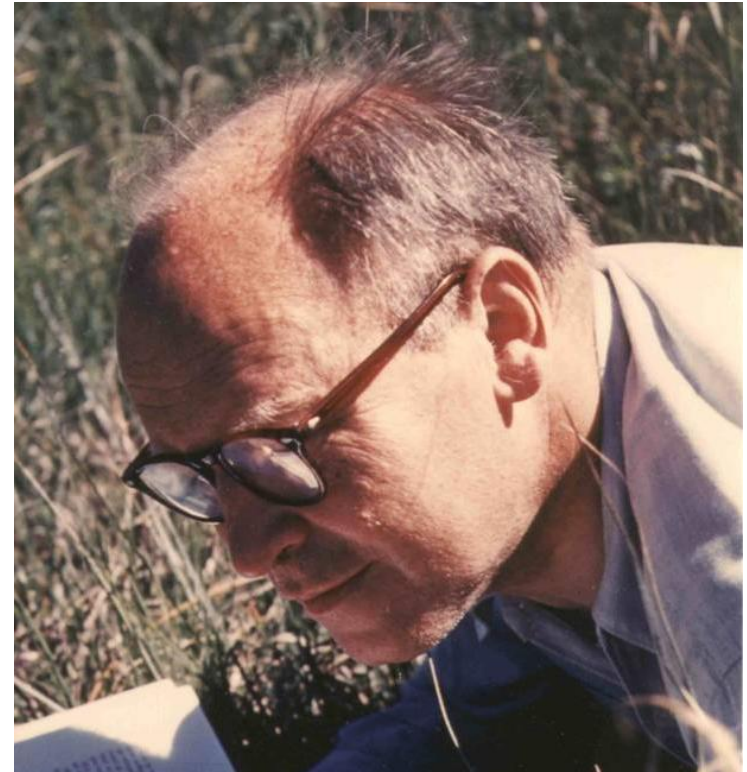
# Group velocity

In summer 1944 Carl Gustaf Rossby, chief meteorological advisor to the US war government, took a well-deserved vacation in the oceanographic research centre La Jolla in southern California





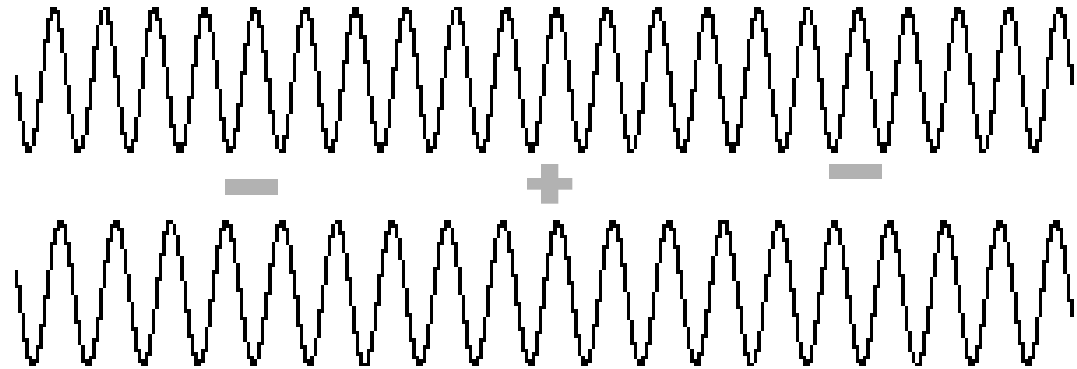
Resting on the beech he  
could listen to the sound  
of the incoming waves,  
their rhythm with a  
peculiar periodicity, “**The  
Seventh Wave**”



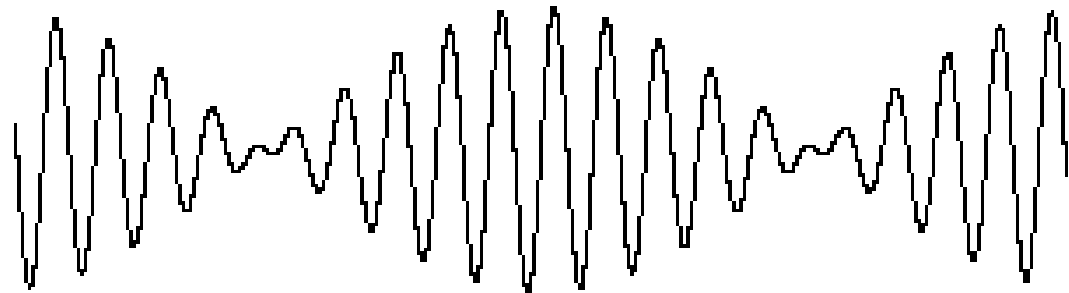
# Group velocity

MADE IN BRITAIN

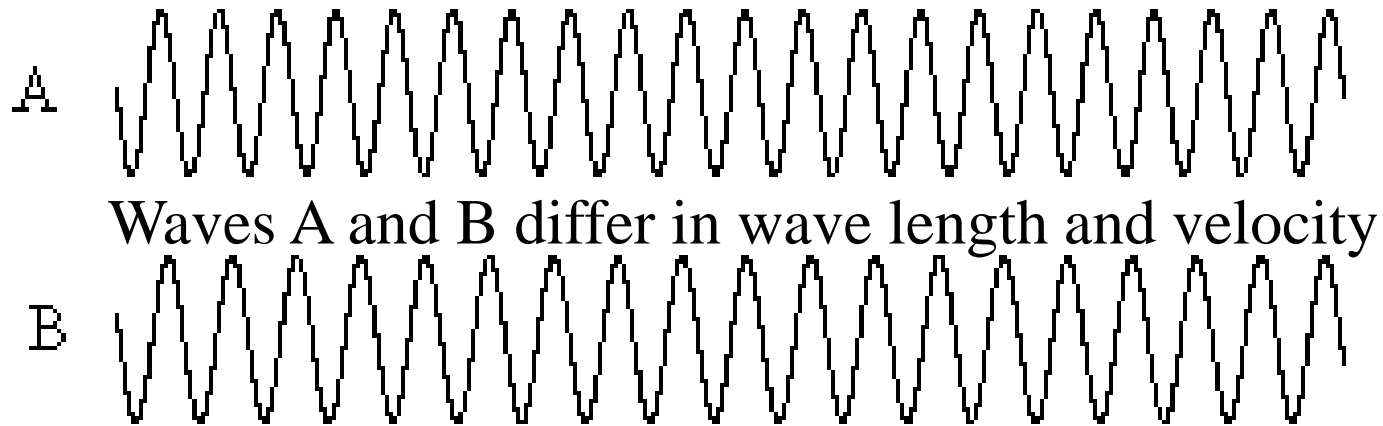
Discovered by Lord Rayleigh



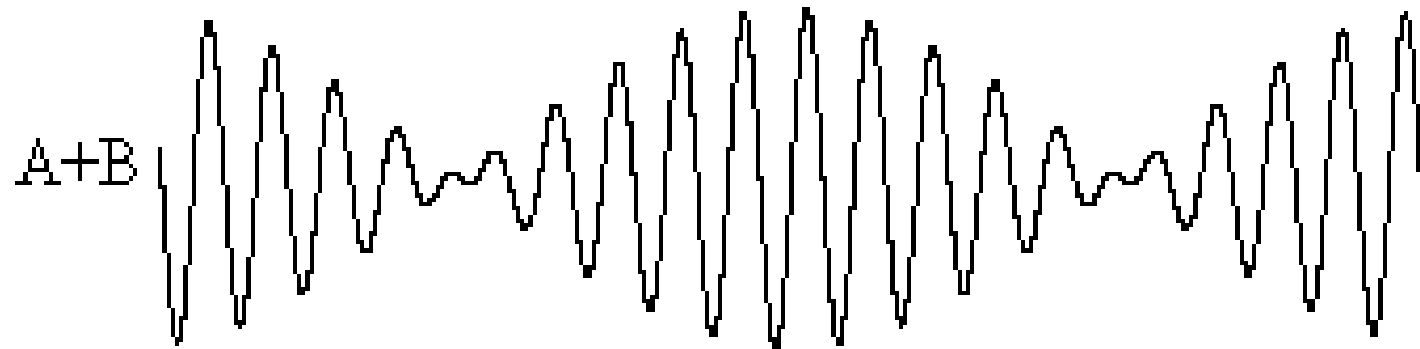
The modulated electromagnetic wave  
can be decomposed into a sum of non-  
modulated waves of different



If the waves' phase speed depend on wave length they are dispersive



The interference wave pattern moves with different velocity to A and B



Suddenly Rossby realised that also “his” newly found wave equation was dispersive

Phase  
speed

$$c = U - \frac{\beta L^2}{4\pi^2}$$

Wave  
length

What is the corresponding group velocity?



Rossby began to derive the group velocity  
- in the sand on the beach!

$$c = U - \frac{\beta L^2}{4\pi^2} \quad \Rightarrow \quad c_g = U + \frac{\beta L^2}{4\pi^2}$$

Phase velocity

Group velocity

## Rossby's wave formula (inspired by Ekman, 1932)

$$c = U - \frac{\beta L^2}{4\pi^2}$$

$C$ = phase speed,  $U$ = zonal flow at 500 hPa,  $L$ =wave length,  $\beta=df/dy$

**$c < 0$  for large  $L$     $c > 0$  for small  $L$**

But what did it mean?

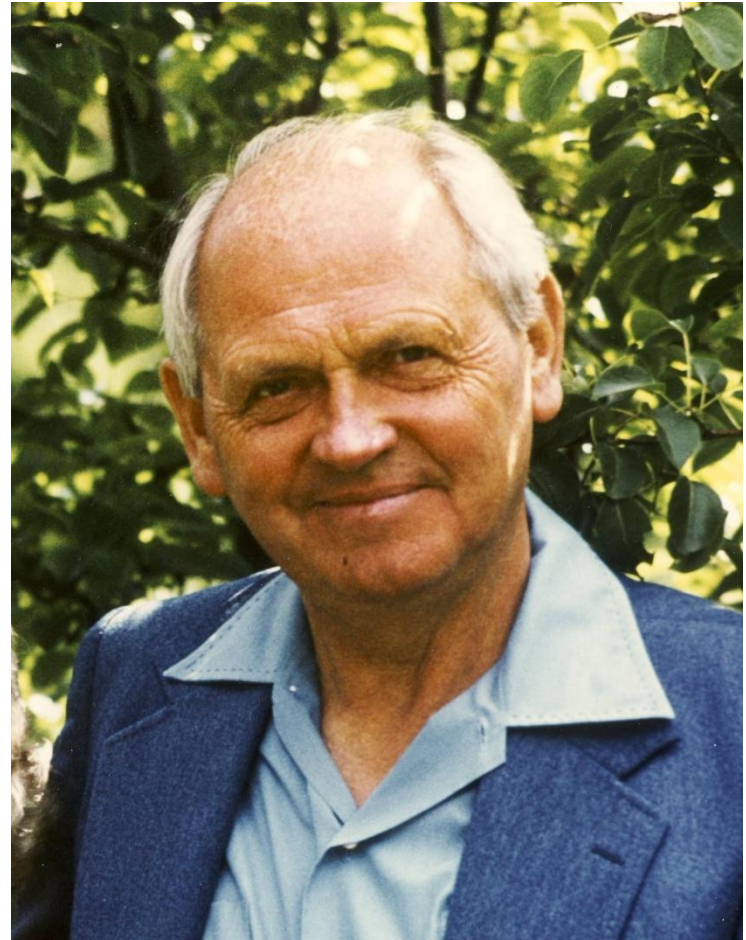
$$c_g = U + \frac{\beta L^2}{4\pi^2}$$

Obviously “something” (the energy) was running rapidly downstream, ahead of synoptic weather systems

## Ernest Hovmöller (1912-2006)

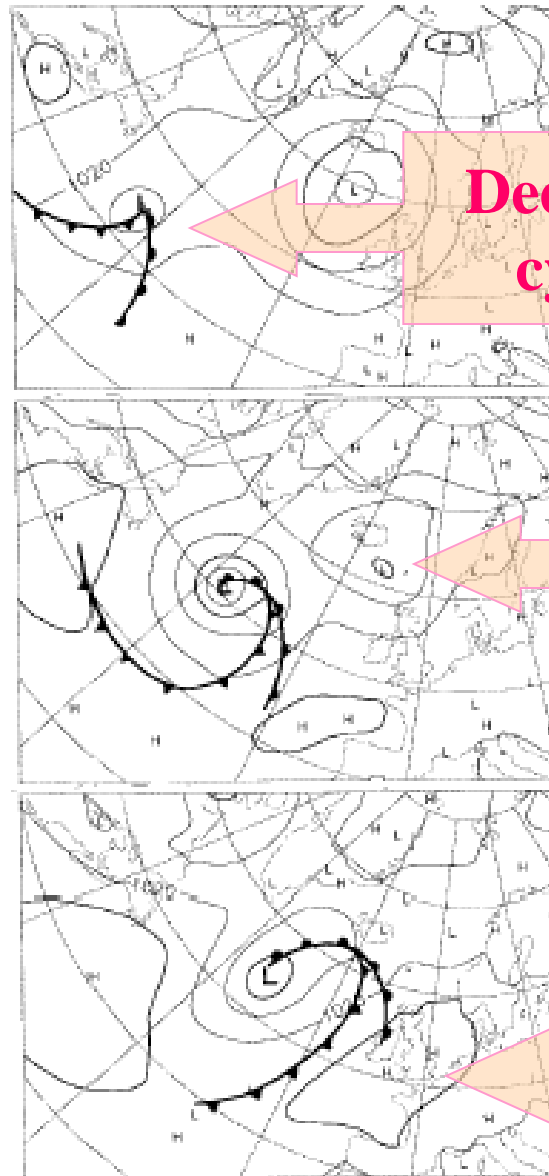
Here the matter  
could have rested

... if it hadn't been  
for this man:



...and his Hovmöller diagram

**An old forecast  
rule about  
downstream  
development  
(Evjen, MetZ, 1936)**



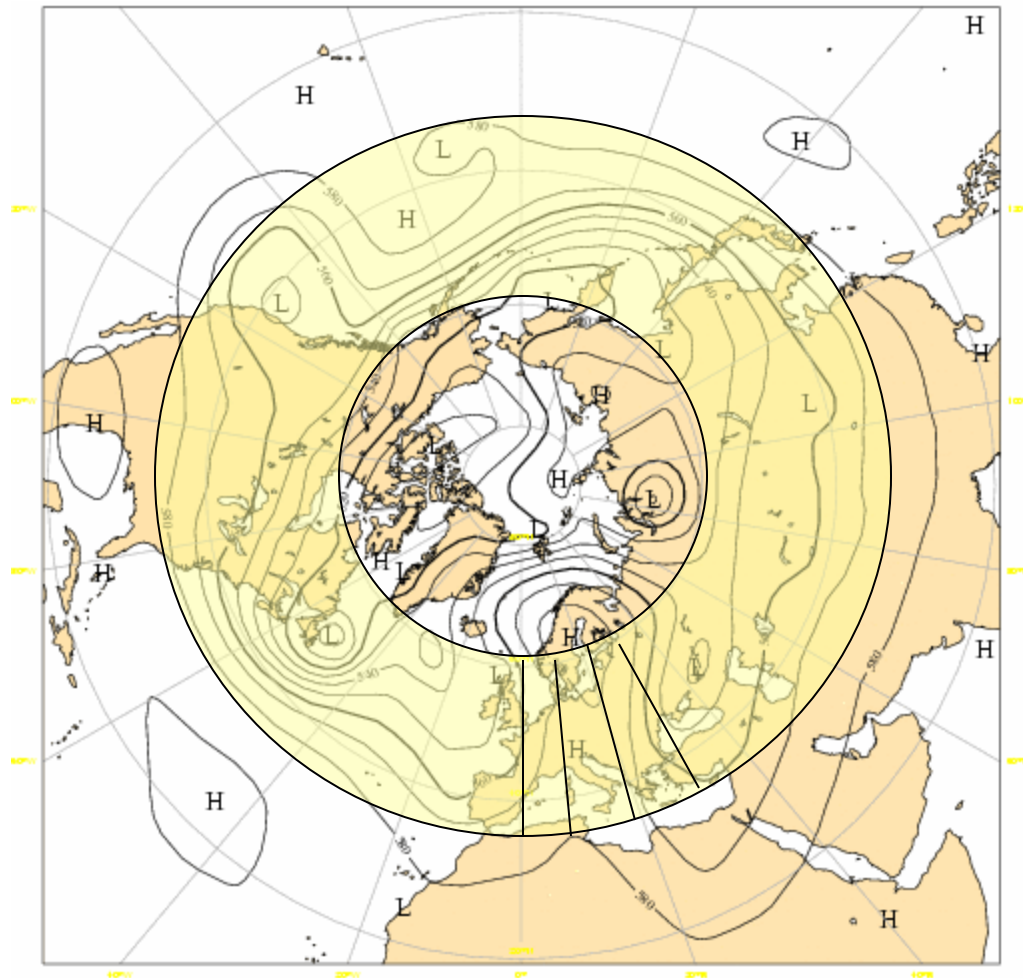
**Deepening  
cyclone**

**Filling low  
pressure system**

**Strengthening  
anticyclone**

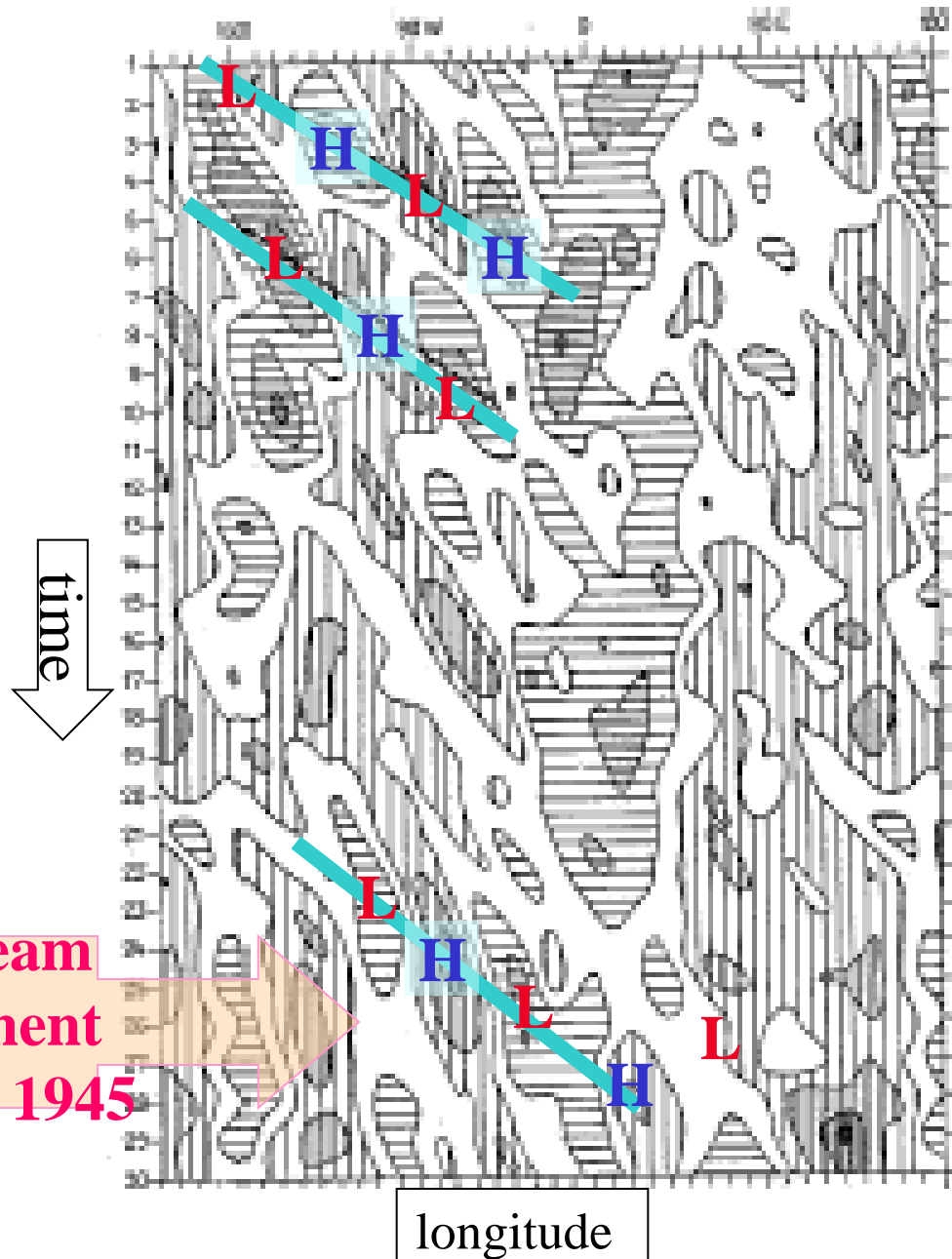


# The traditional Hovmoller diagram - meridional means of 500 hPa heights

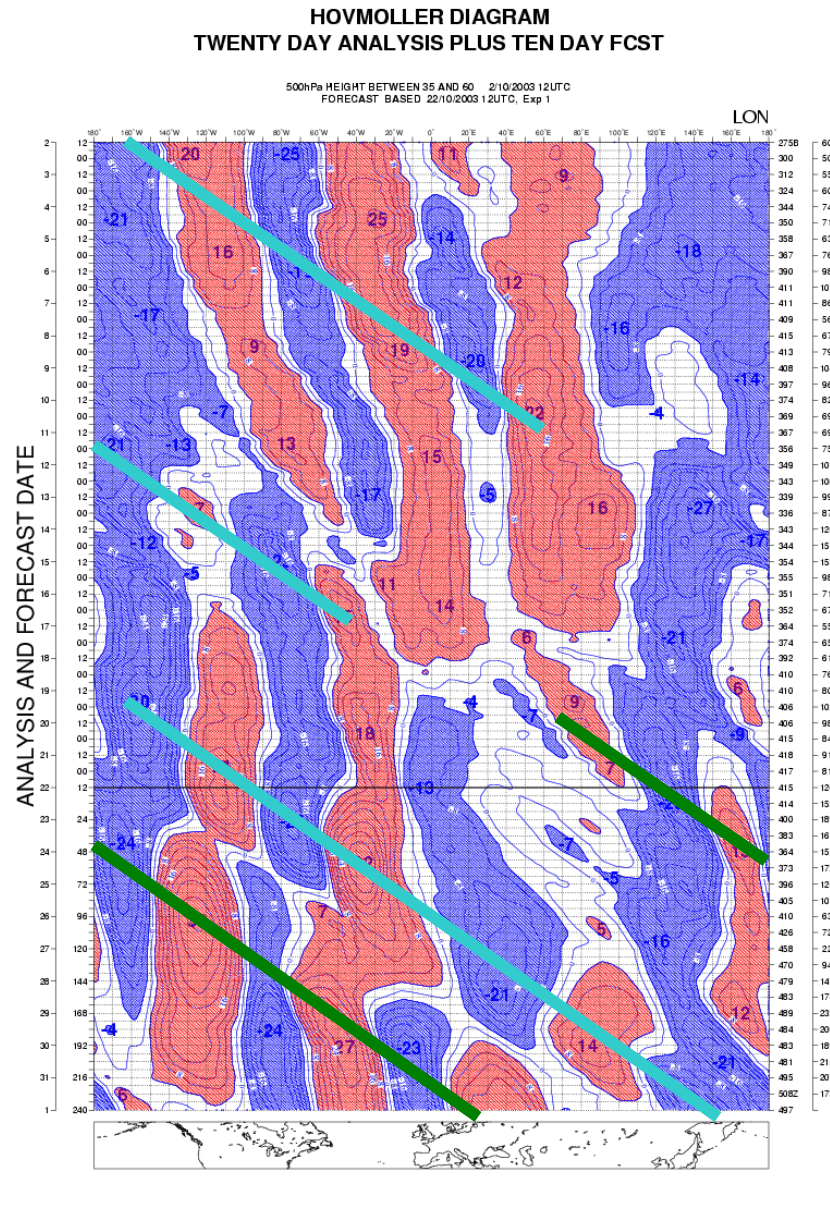


**Hovmöller (1949)**  
made time-  
*longitudinal*  
diagrams of the  
500 hPa height

Downstream  
development  
23-30 Nov 1945



# A routine Hovmöller diagram from ECMEF



# Group velocity in water surface waves

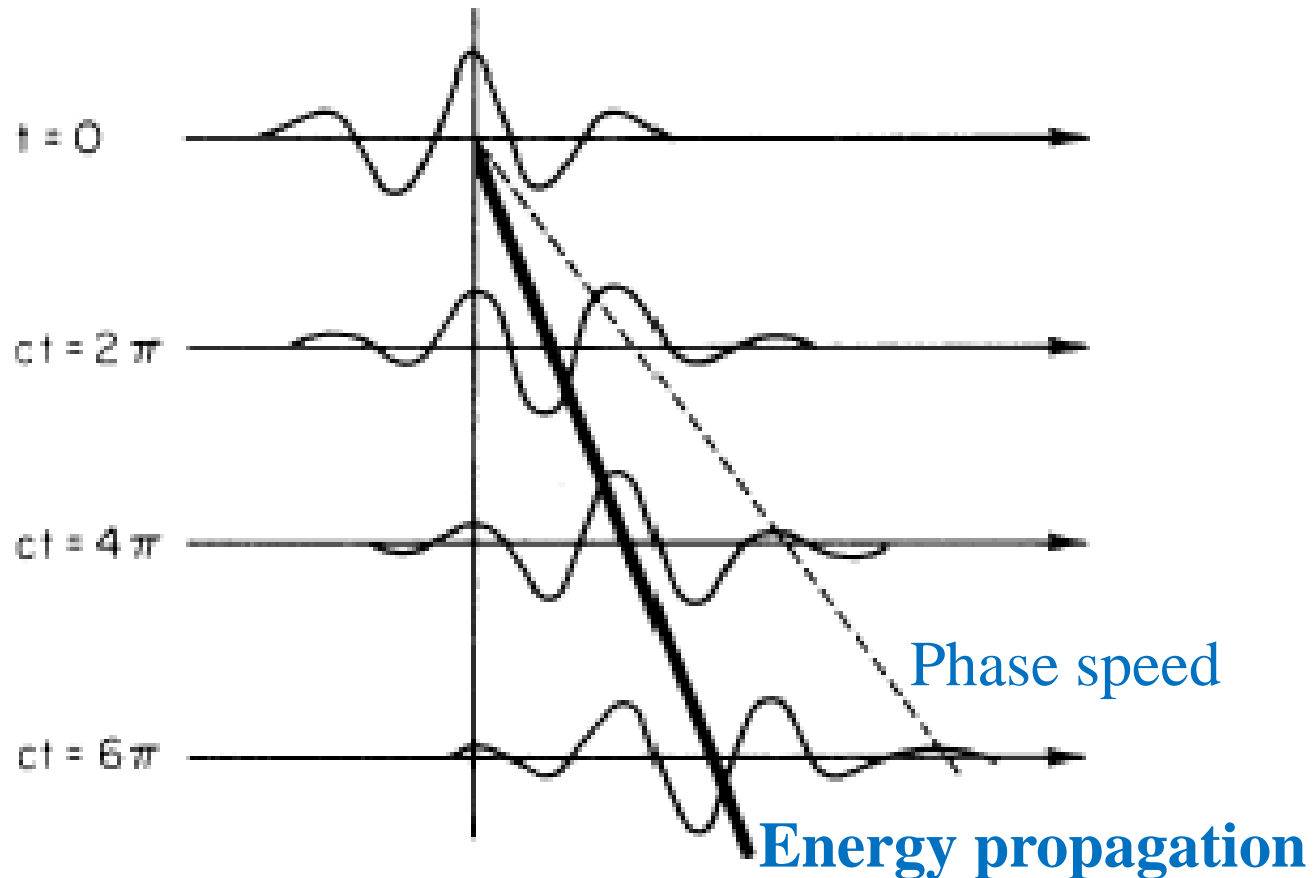
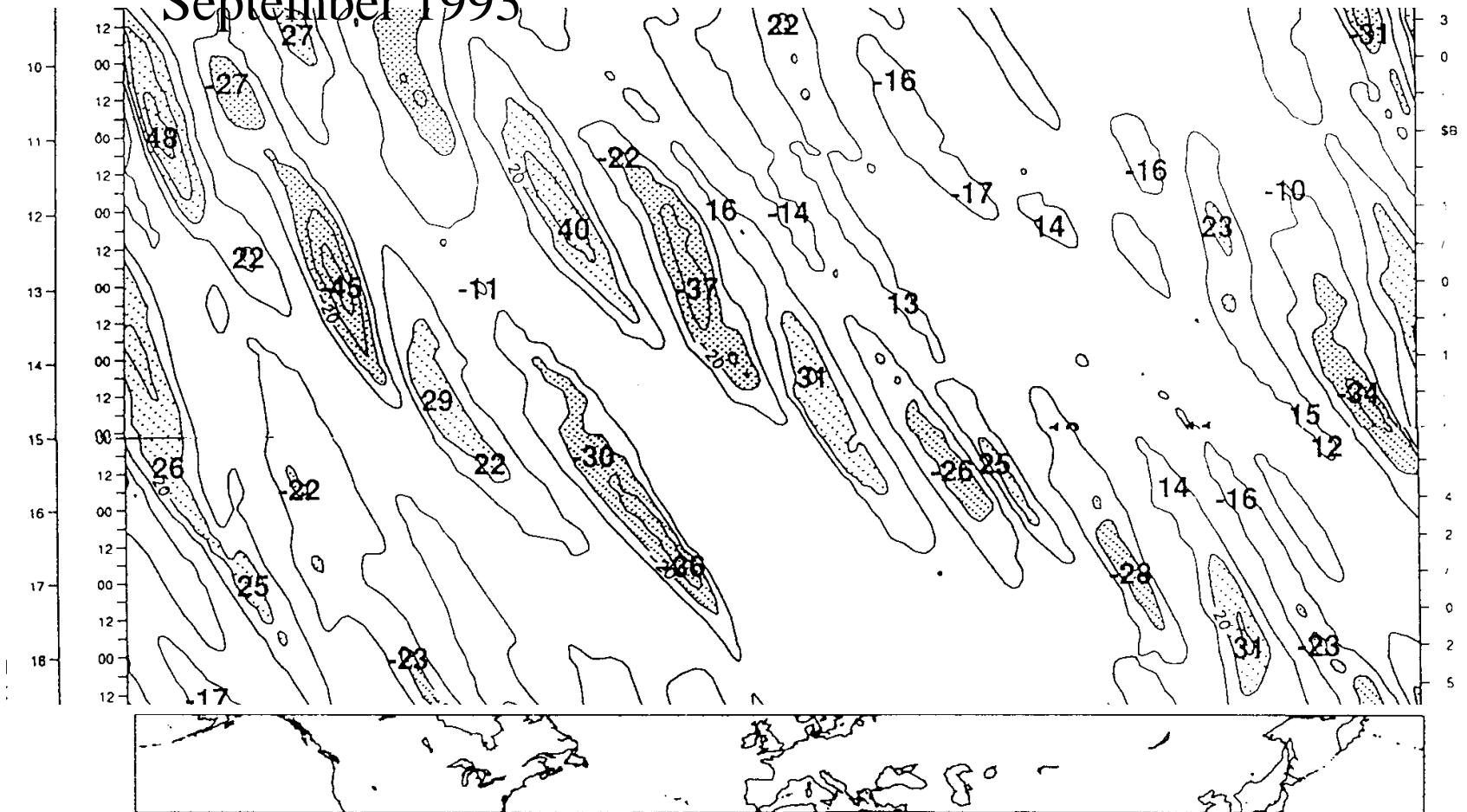


Fig.1 The successive progression of water wave packages. The crest in the centre moves rapidly out, weakens and leaves behind the main energy, into which upstream waves enter and amplify (from Holton, 1992).

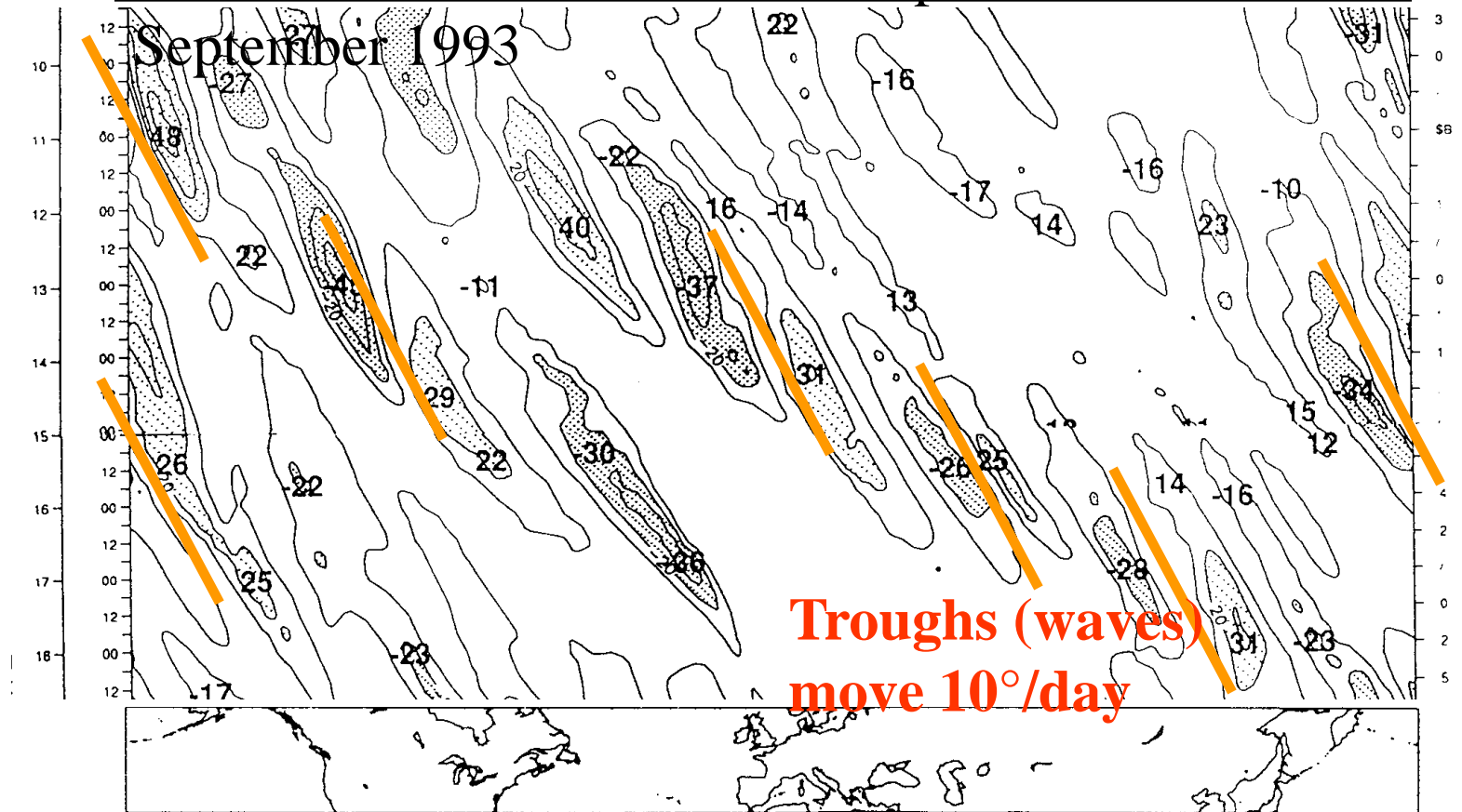
# Trough-ridge (Hovmöller) Diagram of 250 hPa meridional wind component 10-18

September 1993

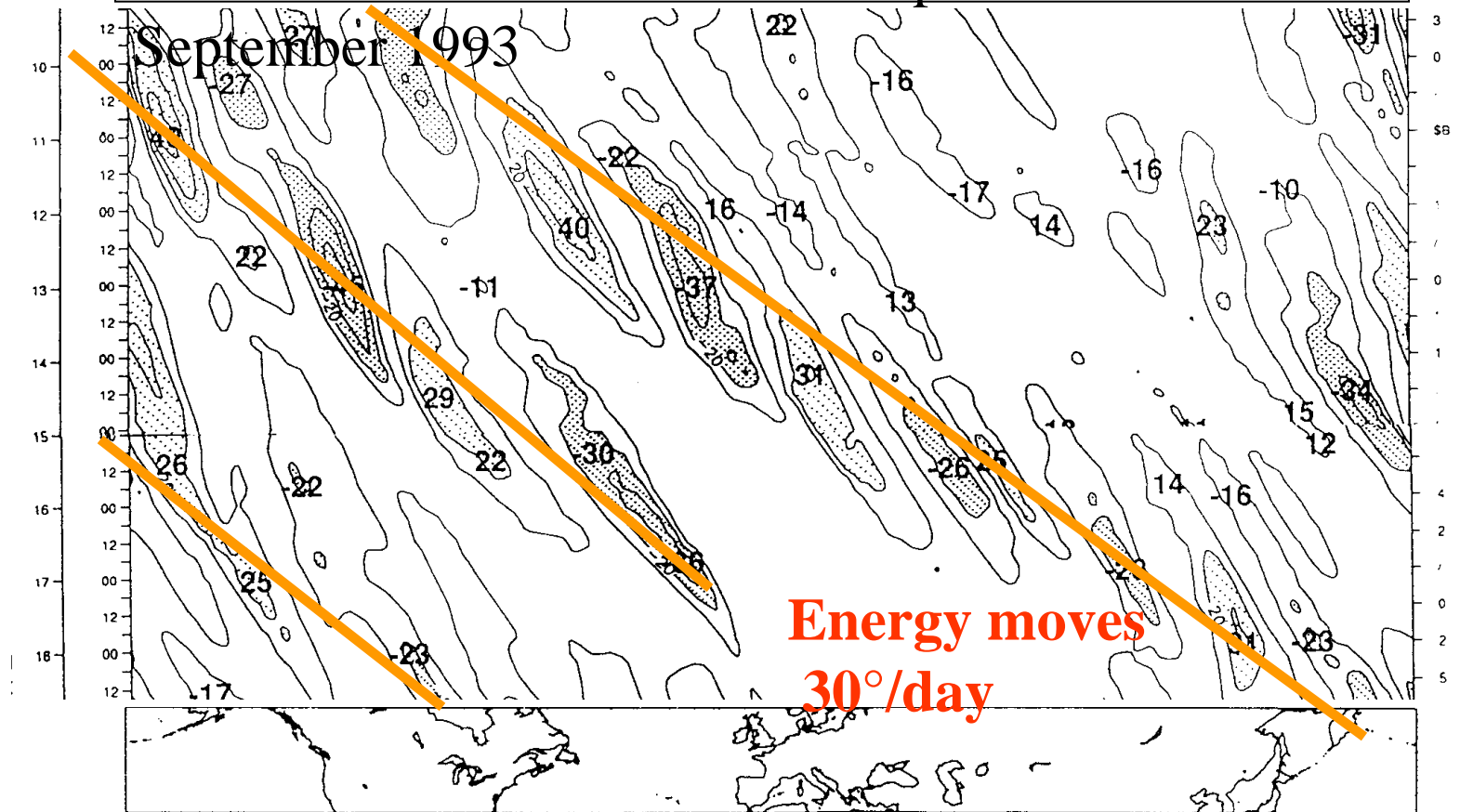




# Trough-ridge (Hovmöller) Diagram of 250 hPa meridional wind component 10-18



# Trough-ridge (Hovmöller) Diagram of 250 hPa meridional wind component 10-18



**From an upstream baroclinic development  
the released kinetic energy is transported,  
through the upper-tropospheric flow,  
to the next downstream cyclone**

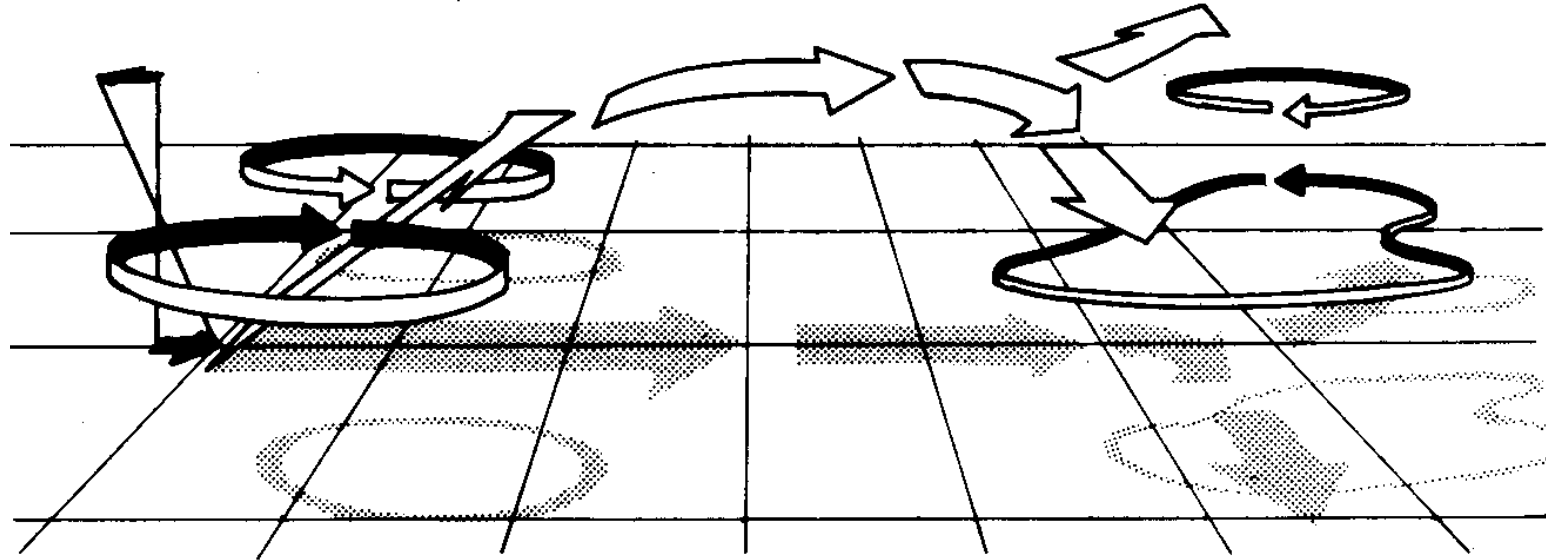


Illustration from Hoskins, James and White (JAS, 1983)

## Group velocity in the atmosphere (Persson, 1993)

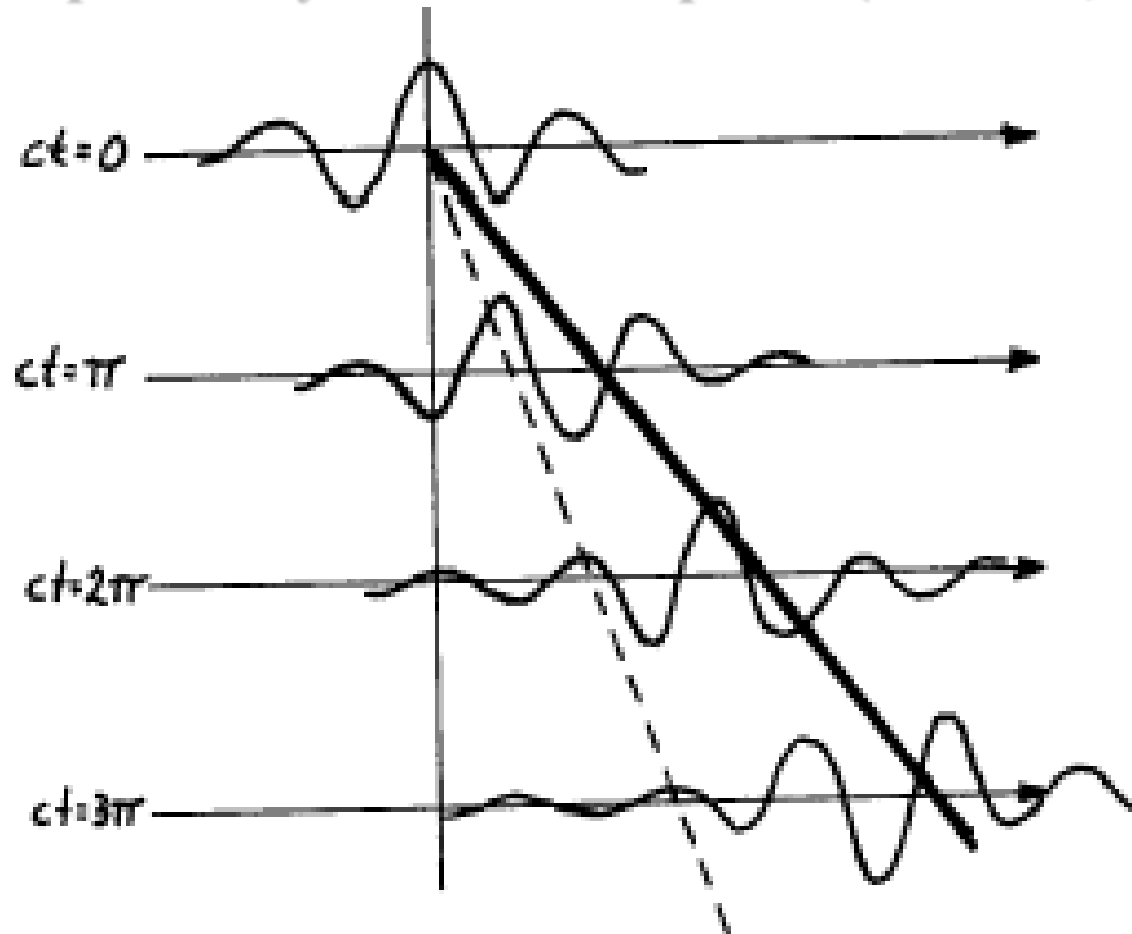
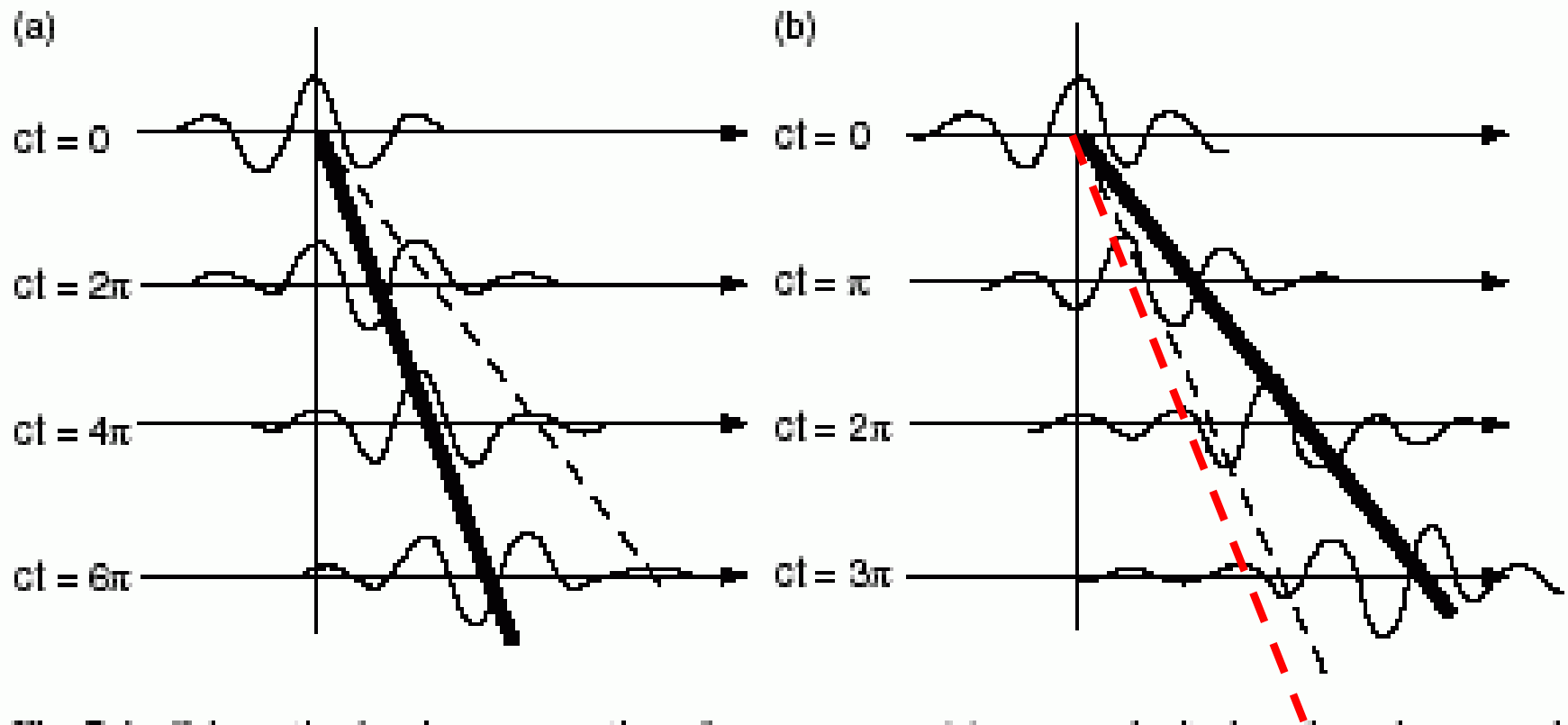


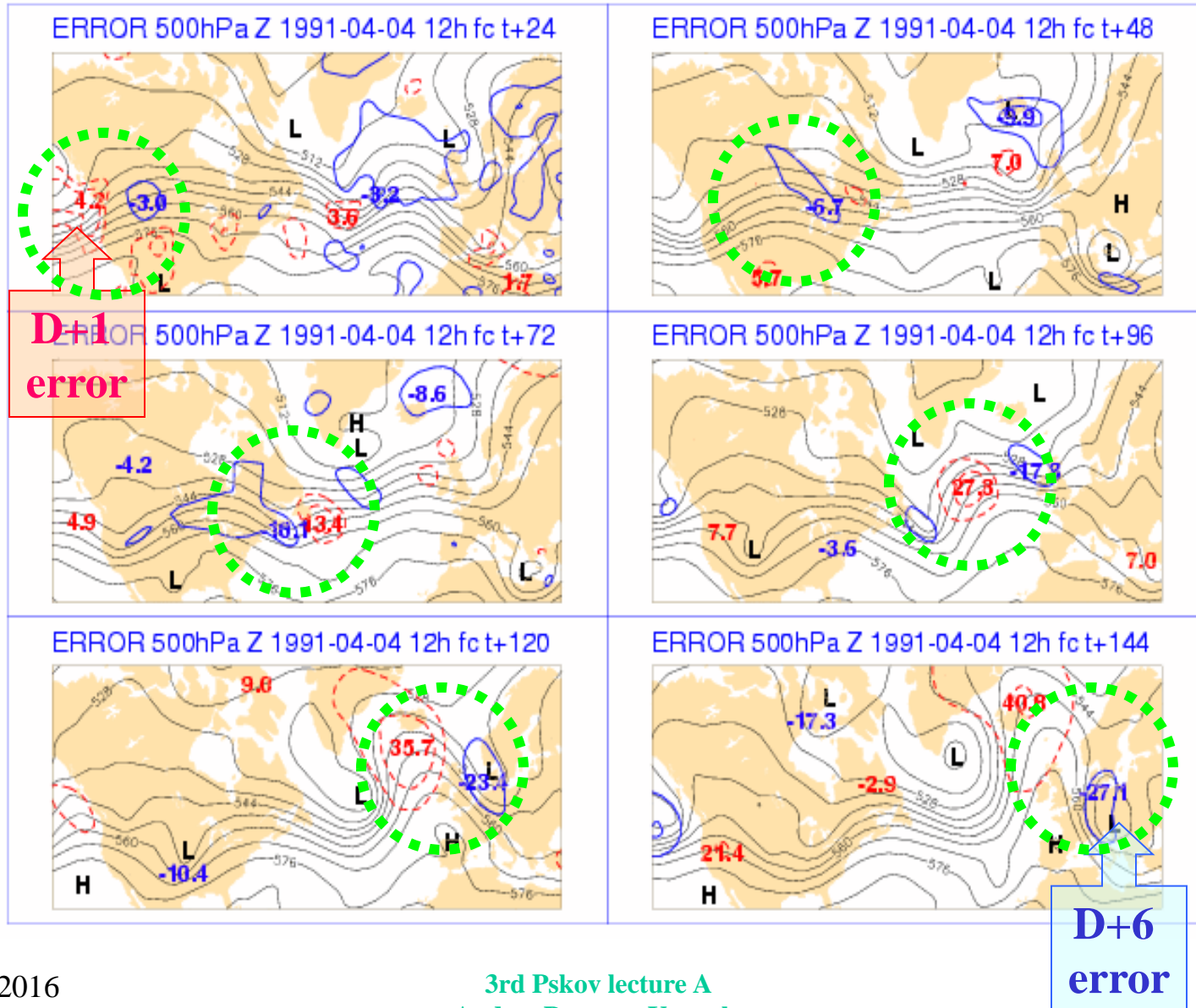
Fig. 2: The corresponding mechanism in the atmosphere: the central wave moves more slowly than the bulk of the energy which propagates downstream amplifying waves on its arrival.

**A relevant image at last made it into the 4th edition  
of James R. Holton's textbook in 2004**



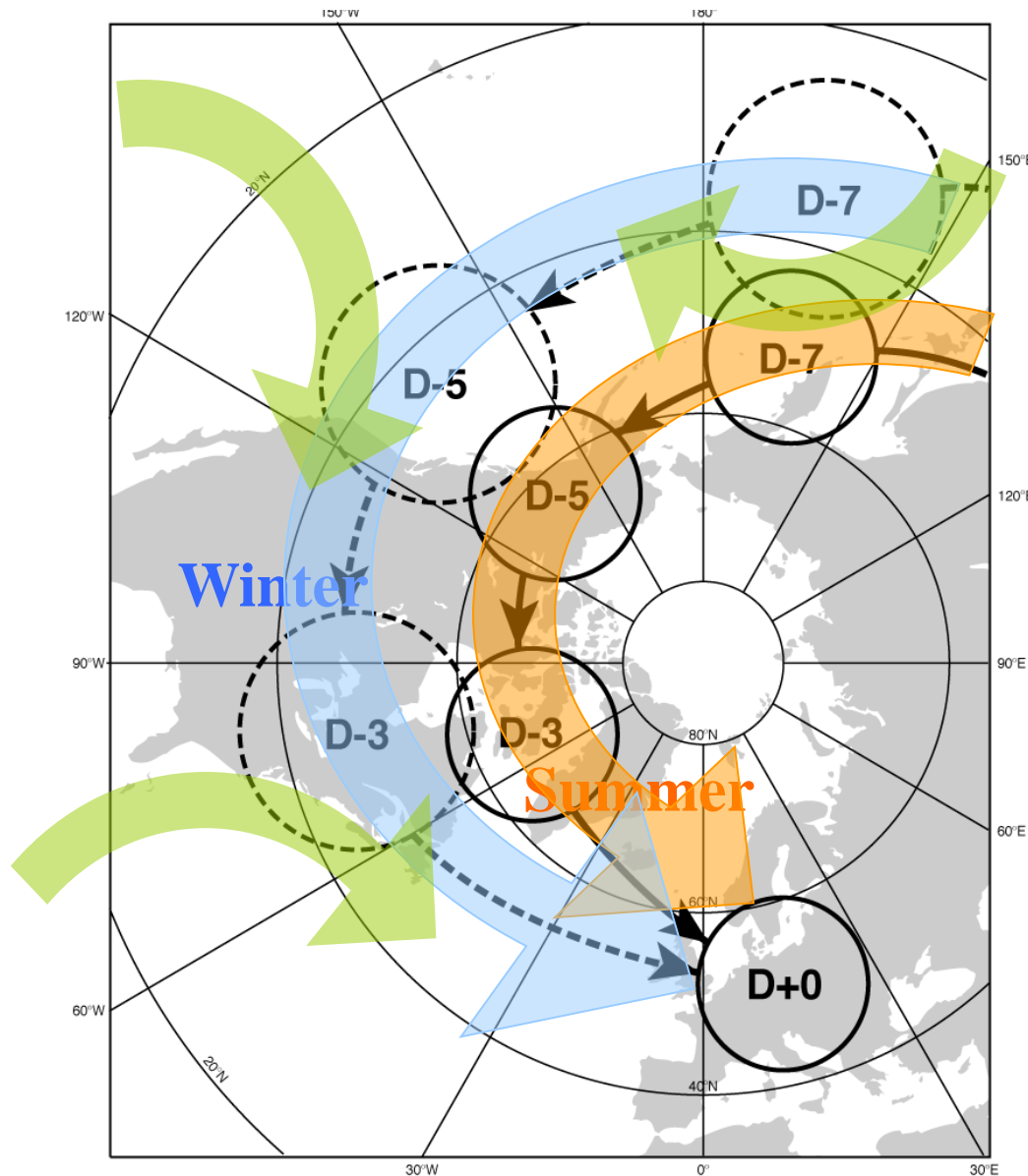
**Fig. 7.4** Schematic showing propagation of wave groups: (a) group velocity less than phase speed and (b) group velocity greater than phase speed. Heavy lines show group velocity, and light lines show phase speed.

# Error tracking from the NE Pacific to Europe in 6 days





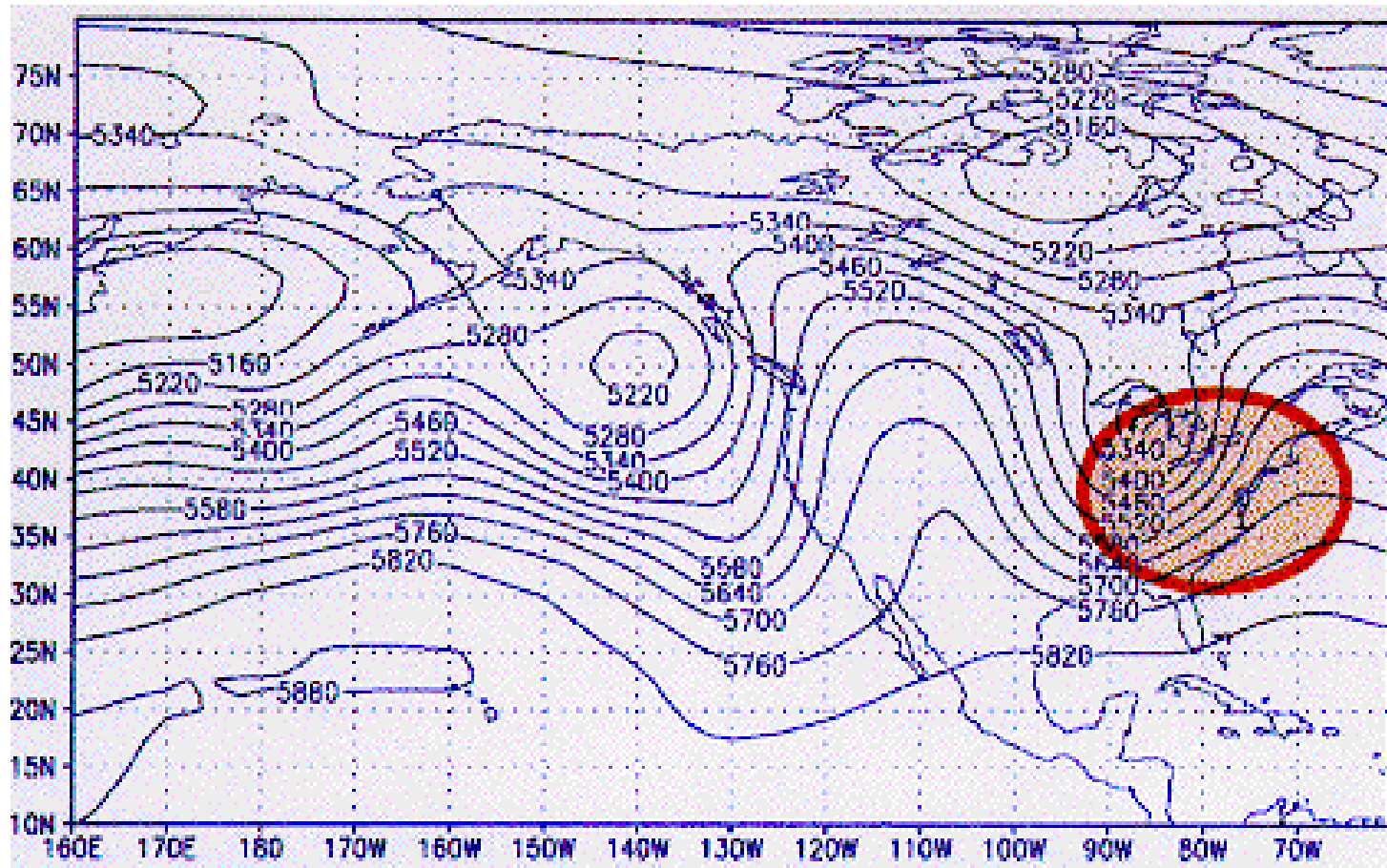
# Error influence over Europa



**Influences of good and bad information move 3 times faster than the weather systems themselves**

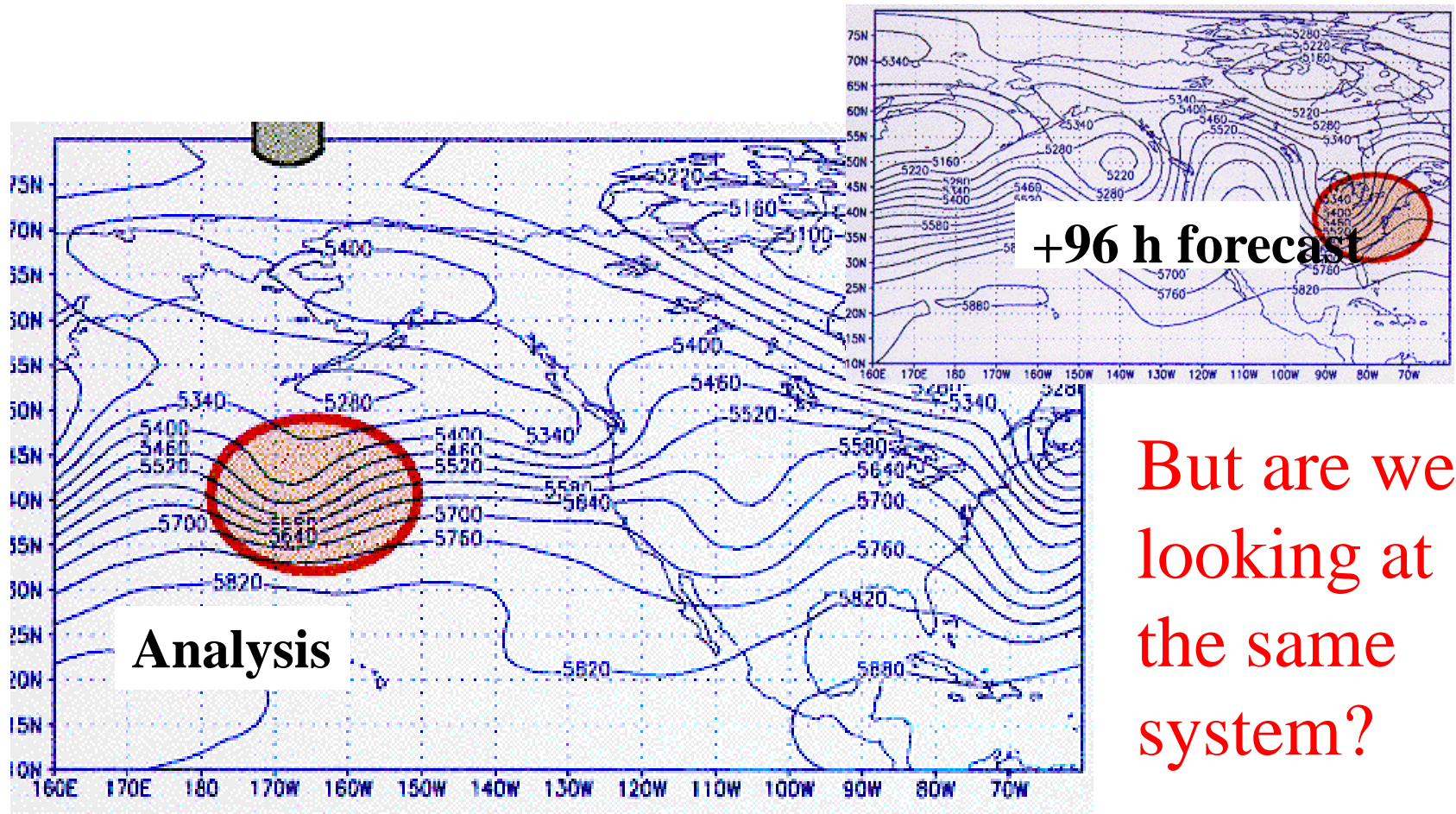
**Add to that tropical cyclones which occasionally move to higher latitudes and radically affect the dynamic developments**

## An example from the NCEP by Zoltan Toht



A numerical +96 h forecast indicates a storm over eastern USA in four days time

Mathematical (adjoint or sensitivity) analyses point out a trough in the mid-Pacific as the likely target for extra observations. More and better observation here will improve the forecast.

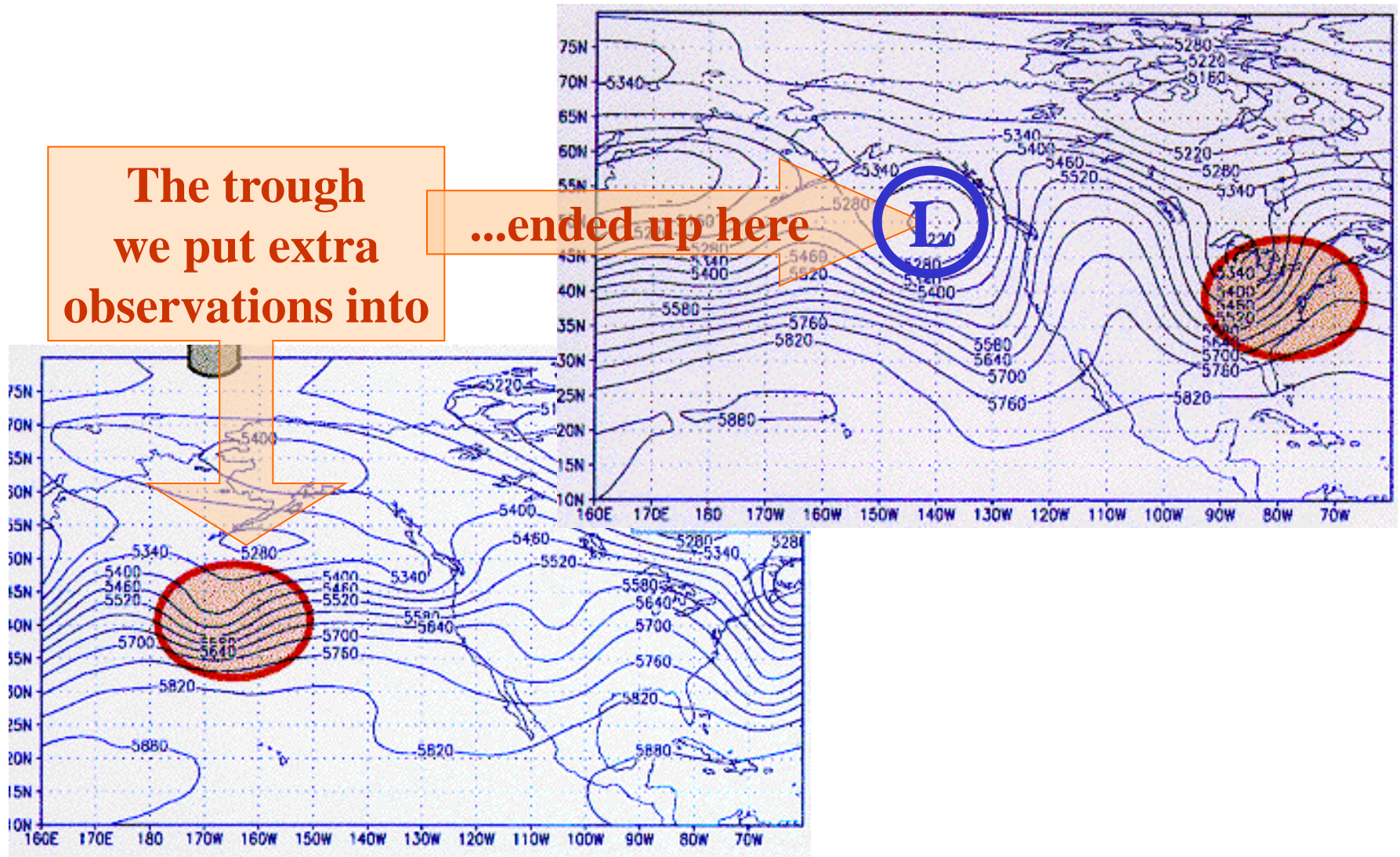


But are we looking at the same system?

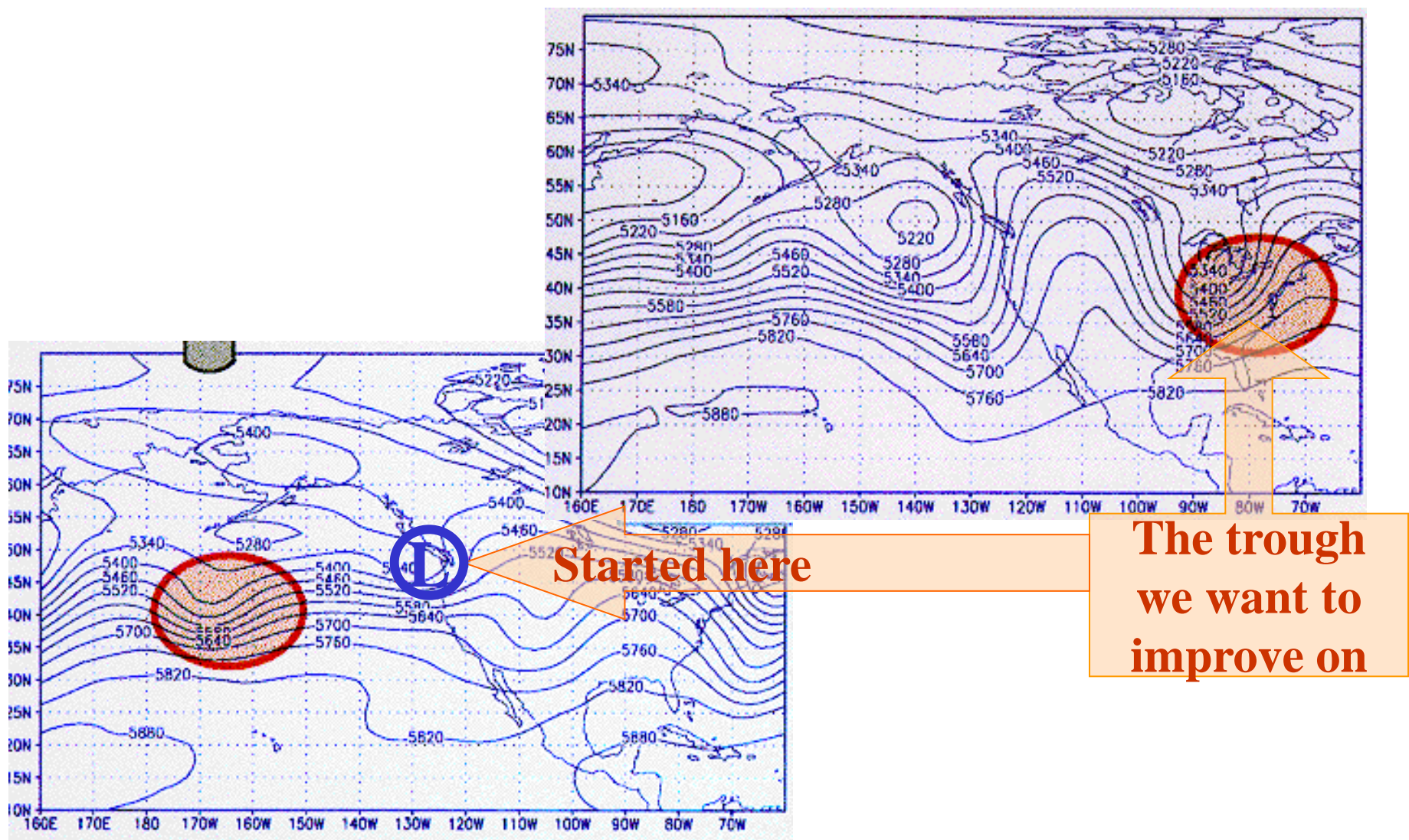
# The answer is NO

The trough  
we put extra  
observations into

...ended up here







# Break